12-07-2023 **EECS 861** Homework 13

Name Student Number

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1. We want to estimate a received signal X from K observations of Y where Y is modeled as Y=X+N. Here, K=20 and

$$\bar{y} = \frac{1}{20} \sum_{i=1}^{20} y_i$$

N is Gaussian with  $N(0, \sigma_N^2)$ X is Gaussian with  $N(12, \sigma_X^2)$ 

N and X are S.I., For the following 3 cases:

Case 1. 
$$\sigma_N^2 = 0.1$$
,  $\sigma_X^2 = 15$   
Case 2.  $\sigma_N^2 = 15$ ,  $\sigma_X^2 = 15$   
Case 3.  $\sigma_N^2 = 15$ ,  $\sigma_X^2 = 0.1$ 

Case 2. 
$$\sigma_N^2 = 15$$
,  $\sigma_X^2 = 15$ 

Case 3. 
$$\sigma_N^2 = 15$$
,  $\sigma_X^2 = 0.1$ 

a. The MAP estimator for X.

1. 
$$\theta_{MAP} = 18$$
  
2.  $\theta_{MAP} = 17.7143$   
3.  $\theta_{MAP} = 12$ 

