



# Computer Vision and Probabilistic Inference

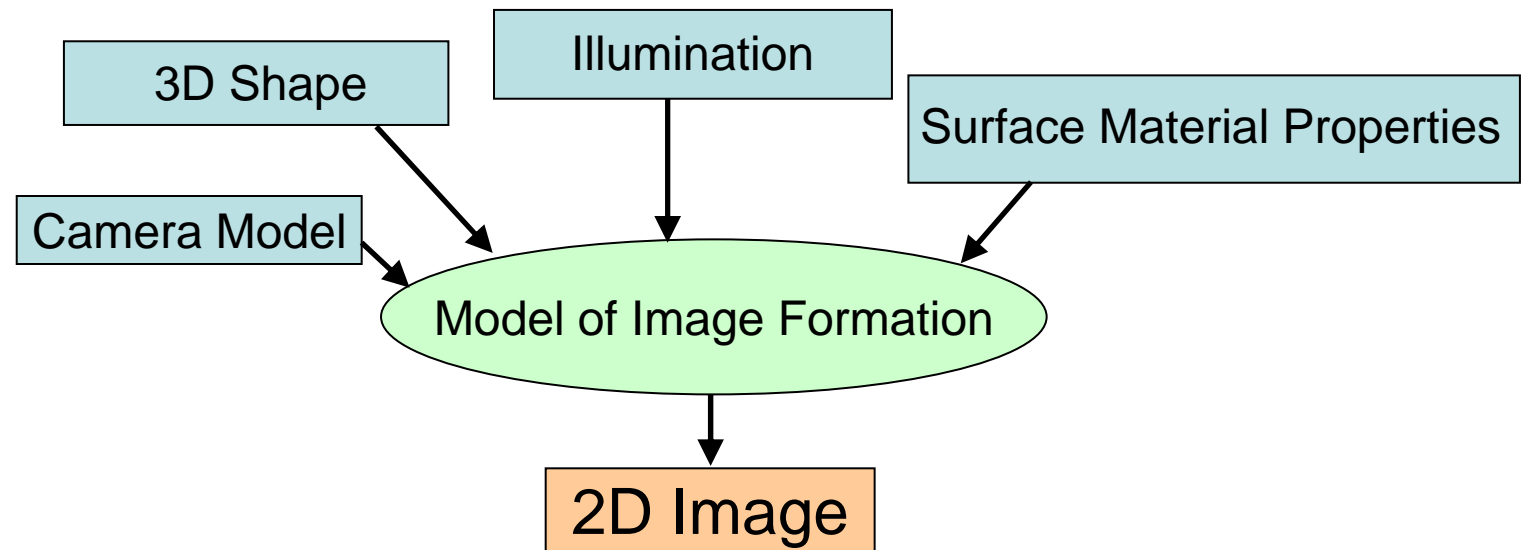
Brian Potetz

# Inference of Depth:

Ambiguous, Underconstrained, Difficult

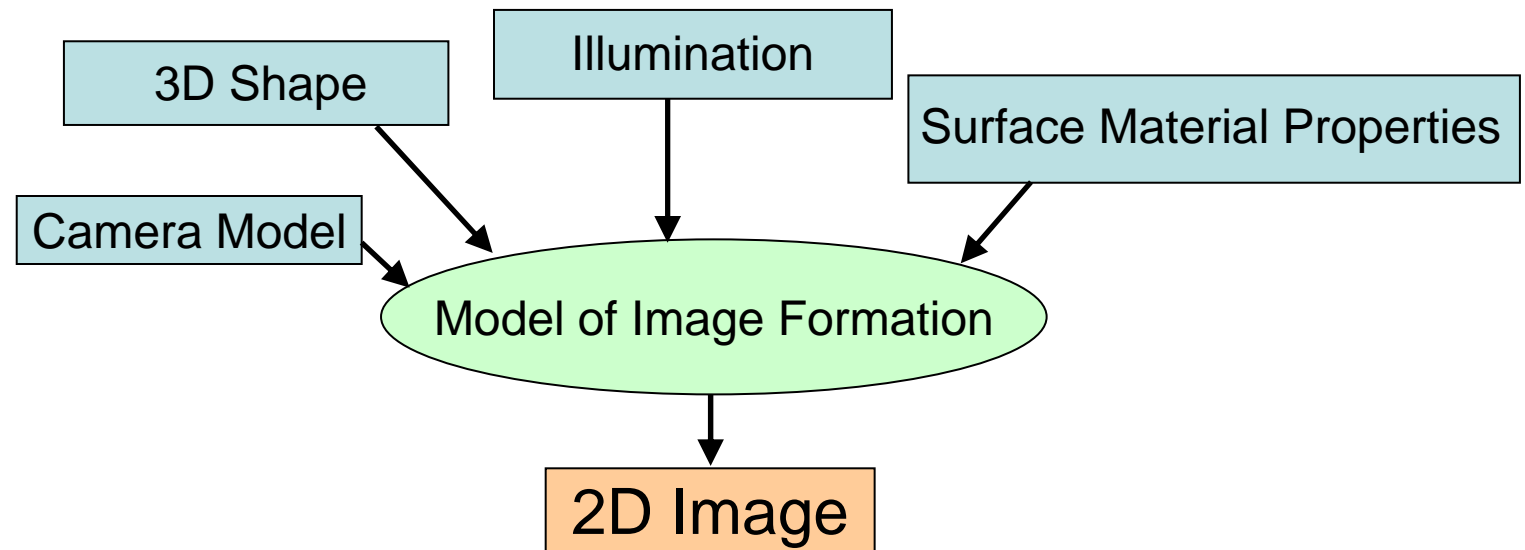
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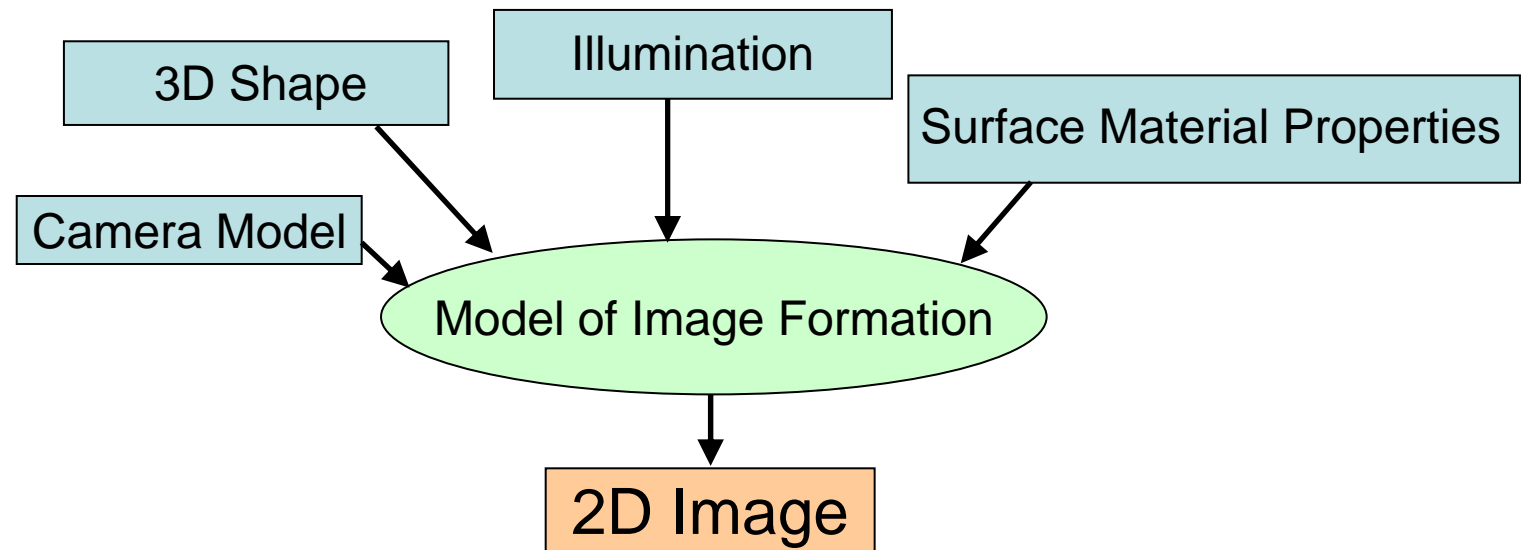


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# Background: Statistical Inference

A Better Approach to infer shape:

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Requires finding the **most likely point** of a **complex, high-dimensional** probability distribution:

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- Gradient ascent often struggles with **local maxima**
- Key insight: exploit local *structure* of the problem. Many probability distributions can be **factorized**:

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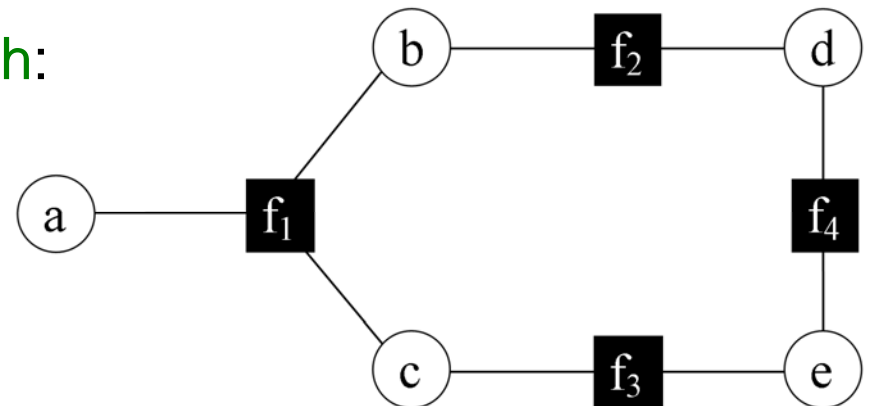
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Example:

$$P(a, b, c, d, e) \propto f_1(a, b, c) f_2(b, d) f_3(c, e) f_4(d, e)$$

Drawn as a **Factor Graph**:

solve using graph  
based algorithms



Applications:

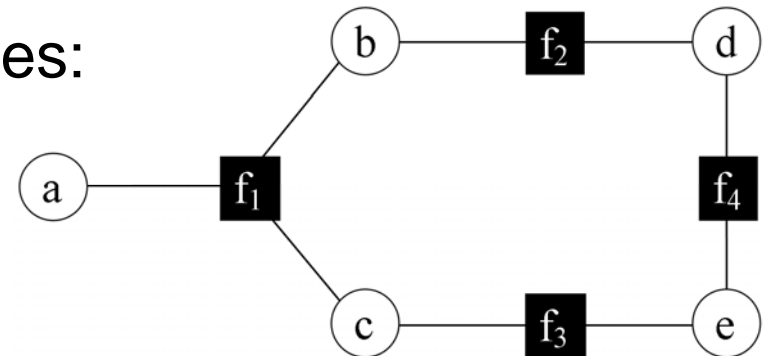
- speech recognition
- disease diagnosis
- fraud detection
- genetic linkage analysis
- error-correcting codes
- data compression
- computer vision

# Belief Propagation

Ex:  $P(a, b, c, d, e) \propto f_1(a, b, c) f_2(b, d) f_3(c, e) f_4(d, e)$

Great empirical successes:

- Error-correcting codes,
- Image super-resolution,
- Shape from stereo,
- Photometric stereo, etc.



Slow for highly connected graphs

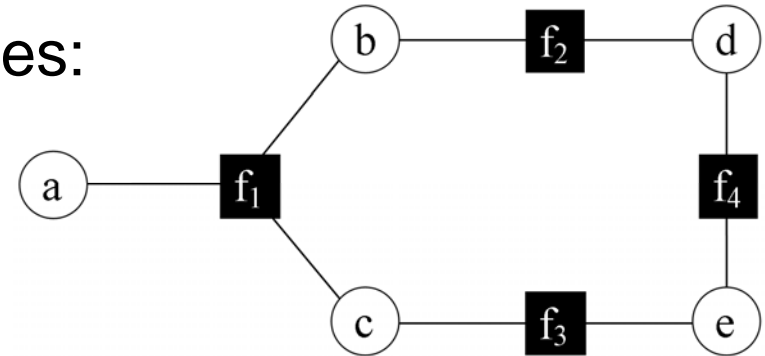
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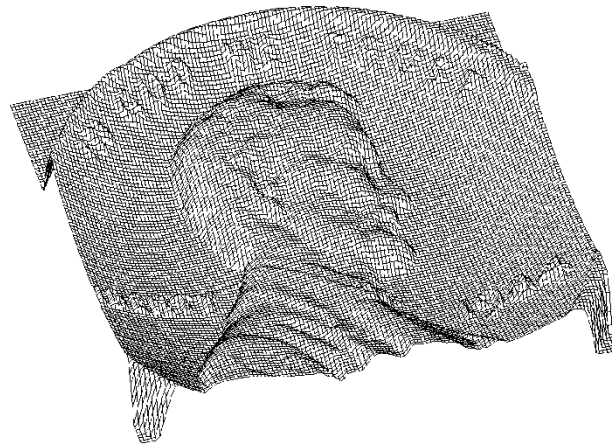
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I have developed a method to reduce complexity (run-time) from exponential to linear.

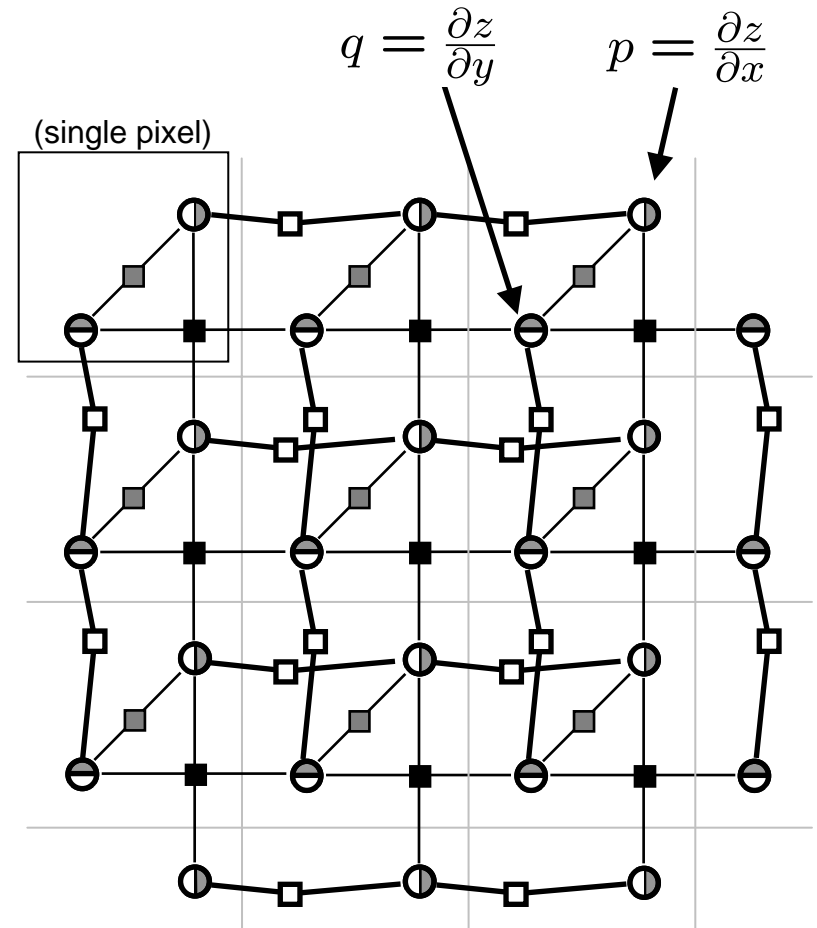
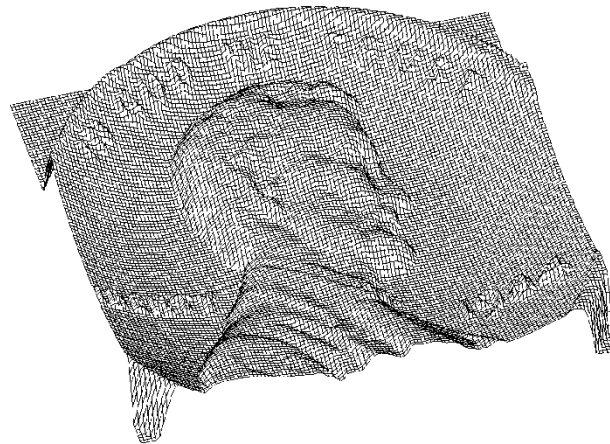
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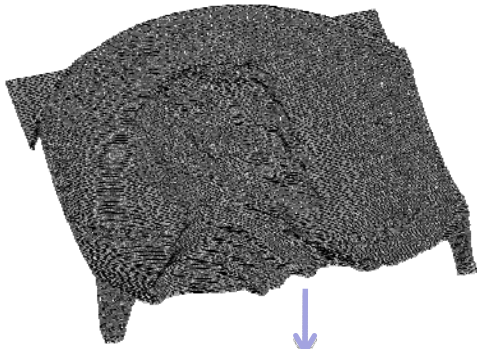
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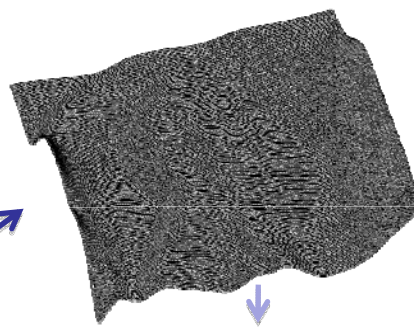
A factorized probability distribution  
for shape-from-shading

# Shape-From-Shading Results

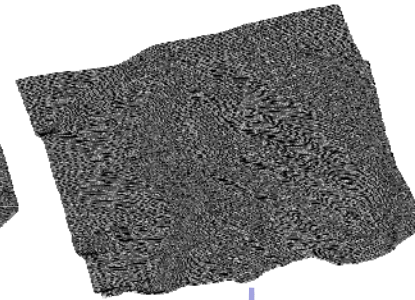
Ground-truth  
3D shape:



Previous state-of-the-art  
algorithms performed poorly:



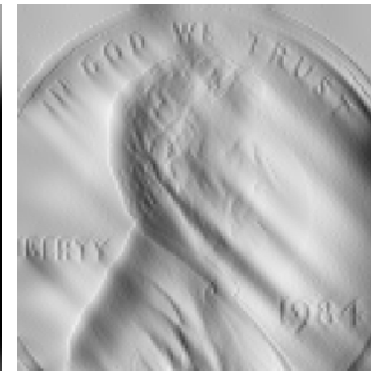
Lee & Kuo



Zheng & Chellappa

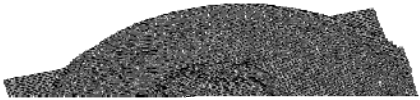


2D Input image



2D images generated by illuminating the reconstructed 3D shapes.

Ground-truth  
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