

EECS 360  
Homework #10

1. Section 5.2 Participation Activities

- 5.2.1: Lowpass and highpass magnitude spectral responses.
- 5.2.2: Bandpass and bandreject magnitude spectral responses.
- 5.2.3: RC circuit lowpass filter (capacitor output).
- 5.2.4: RC circuit highpass filter (resistor output).
- 5.2.6: Ratio to dB conversions.
- 5.2.7: dB to voltage ratio conversions.

2. Exercise 5.2.5

3. Exercise 5.2.6

4. Section 5.3 Participation Activities

- 5.3.1: Examples of bandpass filter responses and Q factor.
- 5.3.2: Designing a bandpass filter for resonant frequency MHz and factor .
- 5.3.5: RLC highpass filter.
- 5.3.7: First order lowpass filter transmission spectrum.

5. Challenge activity

- 5.3.1: Bandpass filters.

6. Section 5.4 Participation Activities

- 5.4.1: Brick-wall lowpass filter response to odd square-wave input.
- 5.4.3: Brick wall filter impulse responses.
- 5.4.4: Brick wall bandpass response to odd square wave.
- 5.4.5: Brick wall bandpass response to rectified sine wave

7. Exercise 5.4.1

8. Let  $H(f) = \text{tri}(f/1000)$

- a. Find the first zero bandwidth.
- b. Find the 3dB bandwidth.
- c. Find the equivalent rectangular bandwidth

9. Let  $x(t) = 10^4 \text{sinc}^2(10^4 \pi t)$  is input to an ideal lowpass filter with a bandwidth of B kHz

- a. Find the smallest B such that the filter introduces no distortion.
- b. Find the % energy in  $x(t)$  in the frequency range  $|f| < 5000\text{Hz}$ ?
- c. What are the barriers to building the filter described in part a)

10. Give  $x(t)$  below with for  $\tau = 0.33\text{ms}$  and  $T_0 = 1.0\text{ms}$ . Design (specify) a system (filter) to convert  $x(t)$  to  $y(t)$   
 $= A \cos(2\pi f_a t + \phi)$  where  $f_a = 2\text{kHz}$  and  $A \neq 0$ .

$$x(t) = \sum_{k=-\infty}^{\infty} \text{rect}\left(\frac{t - kT_0}{\tau}\right)$$

11. Given a pulse  $x(t) = u(t)e^{-\frac{t}{0.01}}$

- a. Find the 6dB bandwidth (in rad/sec and Hz) of this signal.
- b. The signal  $x(t)$  is the input to a ILPF with a bandwidth B (in rad/sec and Hz) to produce an output  $y(t)$ .  
such that  $y(t)$  contains 99% of the energy in  $x(t)$ .

Find E

12. The transfer function for the voltage across the resistor in a series R, L, C circuit is given

$$H(f) = \frac{j2\pi fRC}{1 + j2\pi fRC - LC(2\pi f)^2}$$

- a. Plot  $20\log(|H(f)|)$  with  $R=100\text{ Ohm}$ ,  $L=0.001\text{ Henry}$ ,  $C=0.000001\text{ Farad}$ .
- b. Find the the resonant frequency.
- c. For  $R=100\text{ Ohm}$ ,  $L=0.001\text{ Henry}$ ,  $C=0.000001\text{ Farad}$ , given  $x(t) = \cos(2\pi 17375t)$  find A in

$y(t)=A$

$\cos(2\pi 17375t + \phi)$ . What is the attenuation in dB relative to the resonant frequency.

d. Find the 3dB bandwidth of  $H(f)$ .

Hint: use Transfer Function for Series RLC circuit from the class web page.