

EECS 861  
Topics for Test 2  
Fall 2023

Power Spectral Density,  $S_x(f)$

- $E[X(t)]$
- $\text{Var}[X(t)]$
- Bandwidth and correlation time
- % In-band power
- Random sequences

Properties of time averages- Integration of  $X(t)$

- $E[\text{Time Average}]$
- $\text{Var}[\text{Time Average}]$

Independent Increments – Point Processes – Poisson Process

$$\text{Bandwidth- } B_e = \frac{1}{2} \frac{R_{xx}(0)}{S_x(0)}$$

Variance of time averages

- For large  $2B_eT$ , Number of uncorrelated samples in  $T(\text{sec}) \sim 2B_eT$

Ergodicity

Decomposition of RPs

Sampling of random processes

Quantizing

Major classes of RP

- Bandlimited White Noise
- ARMA, output =  $Y[n]$ 
  - $E[Y[n]]$
  - $\text{Var}[Y[n]]$
  - $R_{YY}[k]$

Response of Systems to Random Inputs

- Discrete time systems
- Continuous time systems
- Output power spectral density
- Output autocorrelation functions
- Output S/N

Detection

- MAP rule
- Detector performance,  $P_{\text{false alarm}}$ ,  $P_{\text{Hit}}$ ,  $P_{\text{miss}}$ ,  $P_{\text{error}}$
- Bayes detection with cost
- Neyman-Pearson rule
- ROC