

$$14.18 \quad NM_H = V_{OH} - V_{IH}$$

$$= 0.8V_{DD} - 0.6V_{DD} = 0.2V_{DD}$$

$$NM_L = V_{IL} - V_{OL}$$

$$= 0.4V_{DD} - 0.1V_{DD} = 0.3V_{DD}$$

$$\text{Width of transition region} = V_{IH} - V_{IL}$$

$$= 0.6V_{DD} - 0.4V_{DD} = 0.2V_{DD}$$

For a minimum noise margin of 0.4 V, we have

$$NM_H = 0.4$$

$$\Rightarrow 0.2V_{DD} = 0.4$$

$$\Rightarrow V_{DD} = 2 \text{ V}$$

14.34 For $v_I = +1.5 \text{ V}$, Q_N will be conducting and operating in the triode region while Q_P will be off. Thus, the incremental resistance to the left of node A will be r_{DSN} ,

$$r_{DSN} = \frac{1}{k_n(V_I - V_{tn})}$$

$$= \frac{1}{0.2(1.5 - 0.5)} = 5 \text{ k}\Omega$$

Thus,

$$v_a = 100 \left(\frac{5}{5 + 100} \right)$$

$$= 4.8 \text{ mV}$$

For $v_I = -1.5 \text{ V}$, Q_N will be off but Q_P will be operating in the triode region with a resistance r_{DSP} ,

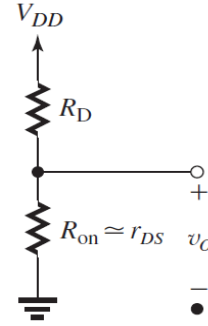
$$r_{DSP} = \frac{1}{k_p(V_{SGP} - |V_{tp}|)}$$

$$= \frac{1}{0.04(1.5 - 0.5)} = 25 \text{ k}\Omega$$

Thus,

$$v_a = 100 \left(\frac{25}{25 + 100} \right) = 20 \text{ mV}$$

14.24



Equivalent circuit for output-low state

The output-high level for the simple inverter circuit shown in Fig. 14.12 of the text is

$$V_{OH} = V_{DD} \Rightarrow V_{DD} = 1.2 \text{ V.}$$

When the output is low, the current drawn from the supply can be calculated as

$$I = \frac{V_{DD}}{R_D + R_{on}} = 30 \mu\text{A}$$

$$\text{Therefore: } R_D + r_{DS} = \frac{1.2}{30 \times 10^{-6}} = 40 \text{ k}\Omega$$

Also:

$$V_{OL} = 0.05 \text{ V} = \frac{r_{DS}}{R_D + r_{DS}} \times V_{DD}$$

$$\Rightarrow r_{DS} = 40 \text{ k}\Omega \times \frac{0.05}{1.2} = 1.67 \text{ k}\Omega$$

$$\text{Hence: } R_D = 40 \text{ K} - 1.67 \text{ K} = 38.3 \text{ k}\Omega$$

$$r_{DS} = \frac{1}{\mu_n C_{ox} \frac{W}{L} (V_{GS} - V_t)}$$

$$= \frac{1}{500 \times 10^{-6} \times \frac{W}{L} (1.2 - 0.4)}$$

$$= 1.67 \text{ k}\Omega$$

$$\Rightarrow \frac{W}{L} = 1.5$$

When the output is low:

$$P_D = V_{DD} I_{DD} = 1.2 \times 30 \mu\text{A} = 36 \mu\text{W}$$

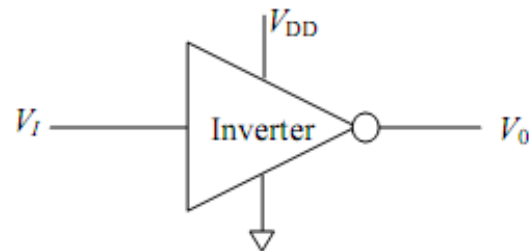
When the output is high, the transistor is off:

$$P_D = 0 \text{ W}$$

Handout problem 1:

An inverter has the transfer function described by

$$V_0 = 2.6 + 2.3 \cos(0.19\pi V_I)$$



If the DC bias voltage is $V_{DD} = 5V$, find V_{IH} , V_{IL} , V_{OH} , V_{OL} , NM_L , and NM_H . (Use $dV_0 / dV_I = -1$ to determine the boundary of regions).

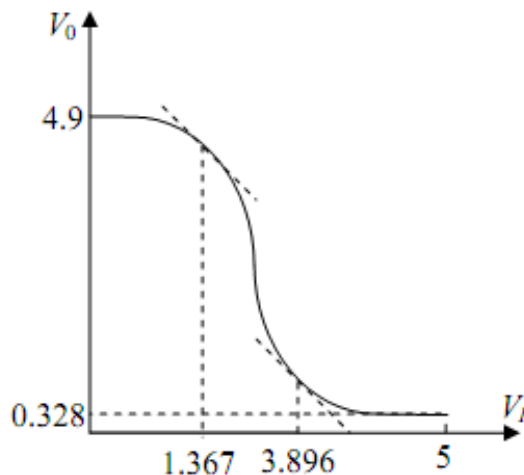
Solution:

Based on the transfer function $V_0 = 2.6 + 2.3 \cos(0.19\pi V_I)$, for $V_I = 0$, $V_0 = 4.9V$, and for $V_I = 5V$, $V_0 = 0.328V$.

To find V_{IH} and V_{IL} , we need to find solutions for $dV_0 / dV_I = -1$.

Since $\frac{dV_0}{dV_I} = -2.3 \times 0.19\pi \sin(0.19\pi V_I) = -1.373 \sin(0.19\pi V_I) = -1$, the solutions are,

$$V_I = 1.367 \text{ and } V_I = 3.896$$



Therefore, $V_{IL} = 1.367$, $V_{IH} = 3.896$, $V_{OL} = 0.328$ and $V_{OH} = 4.9$

$$NM_L = V_{IL} - V_{OL} = 1.367 - 0.328 = 1.039V$$

$$NM_H = V_{OH} - V_{IH} = 4.9 - 3.896 = 1.004V$$

Handout problem 2:

A CMOS inverter has $k = 10\text{mA}/\text{V}^2$, $V_t = 2\text{V}$, $V_{DD} = 6\text{V}$ and an output capacitance of $C = 2\text{nF}$.

(1) Plot the transfer function of $V_o(V_i)$

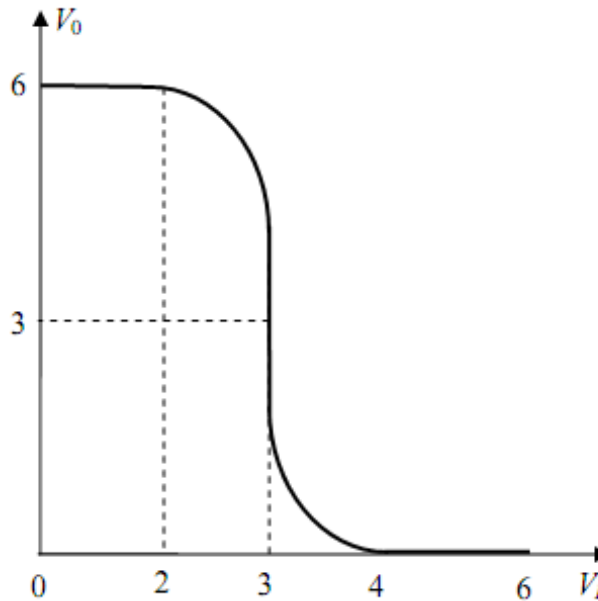
(2) Find t_{PHL}

(3) How do t_{PHL} change if the channel length L of the MOSFET is doubled?

(4) Find the dynamic power dissipation if the CMOS is switched by a signal with 10MHz repetition rate.

Solution:

(1)



(2) Based on equations 14.51 and 14.52:

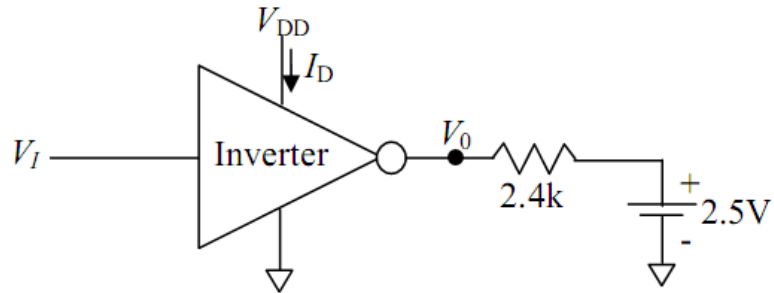
$$t_{PHL} = \frac{2C}{k_n \left[\frac{7}{4} - \frac{3V_t}{V_{DD}} + \left(\frac{V_t}{V_{DD}} \right)^2 \right] V_{DD}} = \frac{2 \times 2 \times 10^{-9}}{10 \left[\frac{7}{4} - \frac{3 \times 2}{6} + \left(\frac{2}{6} \right)^2 \right] \times 6} = \frac{4 \times 10^{-9}}{60 \left[\frac{7}{4} - 1 + \frac{1}{9} \right]} = 77.5\text{ns}$$

(3) Since $t_{PHL} \propto \frac{1}{k_n} = \frac{1}{C_{ox}\mu_n(W/L)} = \frac{L}{C_{ox}\mu_n W}$, if the channel length is doubled, t_{PHL} will be doubled.

(4) Dynamic power dissipation is: $P_D = fCV_{DD}^2 = 10^7 \times 2 \times 10^{-9} \times 6^2 = 0.72\text{W}$

Handout problem 3:

In the following CMOS inverter $k = 2.5\text{mA/V}^2$, $V_t = 1\text{V}$, $V_{DD} = 5\text{V}$.



- (a) Find V_0 if $V_I = 0\text{V}$
- (b) Find V_0 if $V_I = 5\text{V}$
- (c) Find the drain current I_D when $V_I = 2.5\text{V}$

Solution:

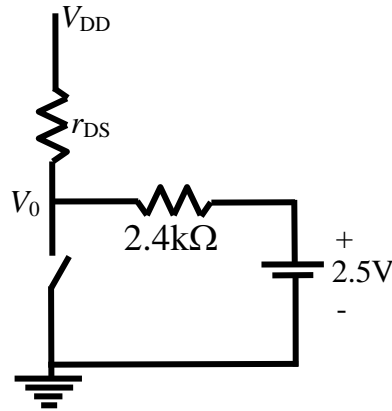
(a) When $V_I = 0$, NMOS (Q_n) is cutoff and PMOS (Q_p) is triode, and the equivalent resistance of Q_p is,

$$r_{DS} = \frac{1}{k_p(V_{DD} - |V_{tp}|)} = \frac{1}{2.5 \times (5 - 1)} = 0.1\text{k}\Omega$$

The current flowing through Q_p is,

$$I_D = \frac{V_{DD} - 2.5}{r_{DS} + 2.4} = \frac{5 - 2.5}{0.1 + 2.4} = 1\text{mA}$$

Then, $V_0 = V_{DD} - I_D r_{DS} = 5 - 1 \times 0.1 = 4.9\text{V}$



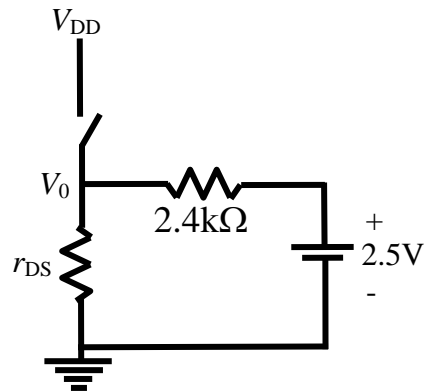
(b) When $V_I = 5\text{V}$, PMOS (Q_p) is cutoff and NMOS (Q_n) is triode, and the equivalent resistance of Q_n is,

$$r_{DS} = \frac{1}{k_n(V_{DD} - V_{tn})} = \frac{1}{2.5 \times (5 - 1)} = 0.1\text{k}\Omega$$

The current flowing through Q_n is,

$$I_D = \frac{2.5}{r_{DS} + 2.4} = \frac{2.5}{0.1 + 2.4} = 1\text{mA}$$

Then, $V_0 = I_D r_{DS} = 1 \times 0.1 = 0.1\text{V}$



(c) When $V_I = 2.5\text{V}$, the output is $V_0 = 2.5\text{V}$ due to the symmetry of the circuit. Both of the two MOSFETs are in saturation mode, and

$$I_D = \frac{k}{2}(V_{GS} - V_t)^2 = 1.25 \times (2.5 - 1)^2 = 2.81\text{mA}$$