

Special Problem 4-6.3

Consider the electric field:

$$\begin{aligned}\mathbf{E}(\bar{r}) = & (3r \sin \theta - 2 \cos \phi) r \hat{a}_r \\ & + \cos \theta (r^{-1} \sin \phi \tan \theta - r^2) \hat{a}_\theta \\ & + \left(\frac{\cos \phi \cot \theta}{r} + r \sin \phi \csc \theta \right) \hat{a}_\phi \quad [V/m]\end{aligned}$$

Determine the electric **potential difference** between point $P_1(r=1, \theta=30^\circ, \phi=0)$ and point $P_2(r=2, \theta=30^\circ, \phi=0)$.

Hint #1: Do **not** attempt to find the electric potential function $V(\bar{r})$!

Hint #2: Do **not** attempt to express $\mathbf{E}(\bar{r})$ in some other coordinate system!