

### Special Problem 5-3.7

A dielectric slab with a thickness of 1.0 m is placed in free space.

The **top** surface of the slab is described as  $-\infty < x < \infty, -\infty < y < \infty, z = 1$ . The **bottom** surface of the slab is described as  $-\infty < x < \infty, -\infty < y < \infty, z = 0$ .

The **relative** dielectric of the slab is given as:

$$\epsilon_{r1}(\bar{r}) = 3 - z$$

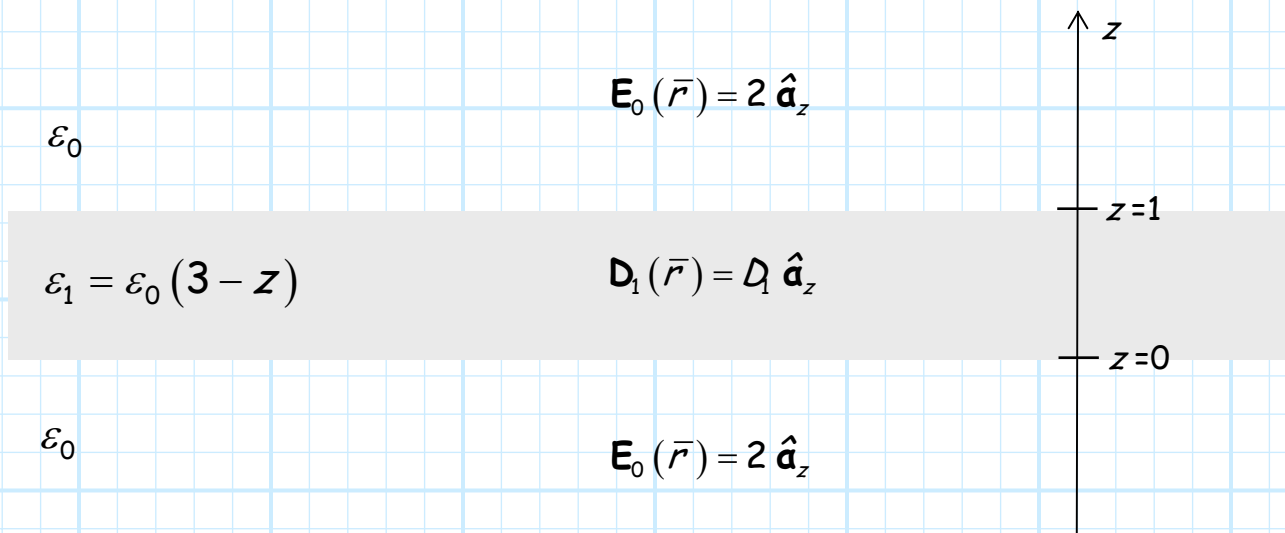
The electric field **above** and **below** the slab (in free space) is:

$$\mathbf{E}_0(\bar{r}) = 2 \hat{\mathbf{a}}_z \quad \left[ \frac{V}{m} \right]$$

The electric flux density **inside** the slab has the form:

$$\mathbf{D}_1(\bar{r}) = D_1 \hat{\mathbf{a}}_z \quad \left[ \frac{V}{m} \right]$$

where  $D_1$  is an unknown **constant**.



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Determine:

1. The value of constant  $D_i$ .
2. The electric field  $\mathbf{E}_1(\vec{r})$  inside the dielectric slab.
3. The **polarization vector** within the dielectric slab.
4. The value of the **polarization** (i.e., **bound**) surface charge density on the **top** surface of the slab.
5. The value of the **polarization** (i.e., **bound**) surface charge density on the **bottom** surface of the slab.