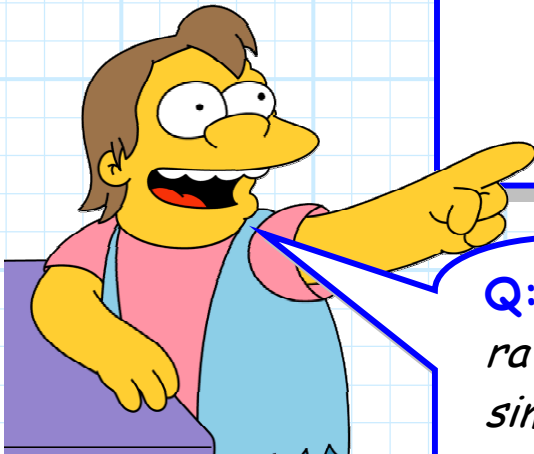


# Line Impedance

Now let's define **line impedance**  $Z(z)$ , which is simply the ratio of the complex line voltage and complex line current:

$$Z(z) = \frac{V(z)}{I(z)}$$



**Q:** *Hey! I know what this is! The ratio of the voltage to current is simply the **characteristic impedance**  $Z_0$ , right ???*

**A:** **NO!** The line impedance  $Z(z)$  is (generally speaking) **NOT** the transmission line **characteristic impedance**  $Z_0$ !!!

→ It is **unfathomably important** that you understand this!!!!

To see why, recall that:

$$V(z) = V^+(z) + V^-(z)$$

And that:

$$I(z) = \frac{V^+(z) - V^-(z)}{Z_0}$$

Therefore:

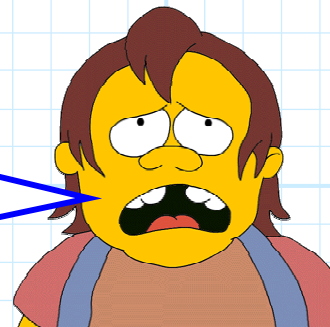
$$Z(z) = \frac{V(z)}{I(z)} = Z_0 \left( \frac{V^+(z) + V^-(z)}{V^+(z) - V^-(z)} \right) \neq Z_0$$

Or, more specifically, we can write:

$$Z(z) = Z_0 \left( \frac{V_0^+ e^{-\gamma z} + V_0^- e^{+\gamma z}}{V_0^+ e^{-\gamma z} - V_0^- e^{+\gamma z}} \right)$$

**Q:** *I'm confused! Isn't:*

$$V^+(z)/I^+(z) = Z_0 ???$$



**A:** Yes! That is true! The ratio of the voltage to current for **each** of the two propagating waves is  $\pm Z_0$ . However, the ratio of the **sum** of the two voltages to the **sum** of the two currents is **not** equal to  $Z_0$  (generally speaking)!

This is actually confirmed by the equation above. Say that  $V^-(z) = 0$ , so that only **one** wave ( $V^+(z)$ ) is propagating on the line.

In this case, the ratio of the **total** voltage to the total current is simply the ratio of the voltage and current of the **one** remaining wave—the **characteristic impedance**  $Z_0$ !

$$Z(z) = \frac{V(z)}{I(z)} = Z_0 \left( \frac{V^+(z)}{I^+(z)} \right) = \frac{V^+(z)}{I^+(z)} = Z_0 \quad (\text{when } V^+(z))$$

**Q:** *So, it appears to me that characteristic impedance  $Z_0$  is a **transmission line parameter**, depending **only** on the transmission line values  $R$ ,  $G$ ,  $L$ , and  $C$ .*

*Whereas **line impedance** is  $Z(z)$  depends the magnitude and phase of the two propagating waves  $V^+(z)$  and  $V^-(z)$ --values that depend **not only** on the transmission line, but also on the two things **attached** to either **end** of the transmission line!*

*Right !?*



**A:** **Exactly!** Moreover, note that characteristic impedance  $Z_0$  is simply a **number**, whereas line impedance  $Z(z)$  is a **function** of position ( $z$ ) on the transmission line.