

Microwave Filter Design

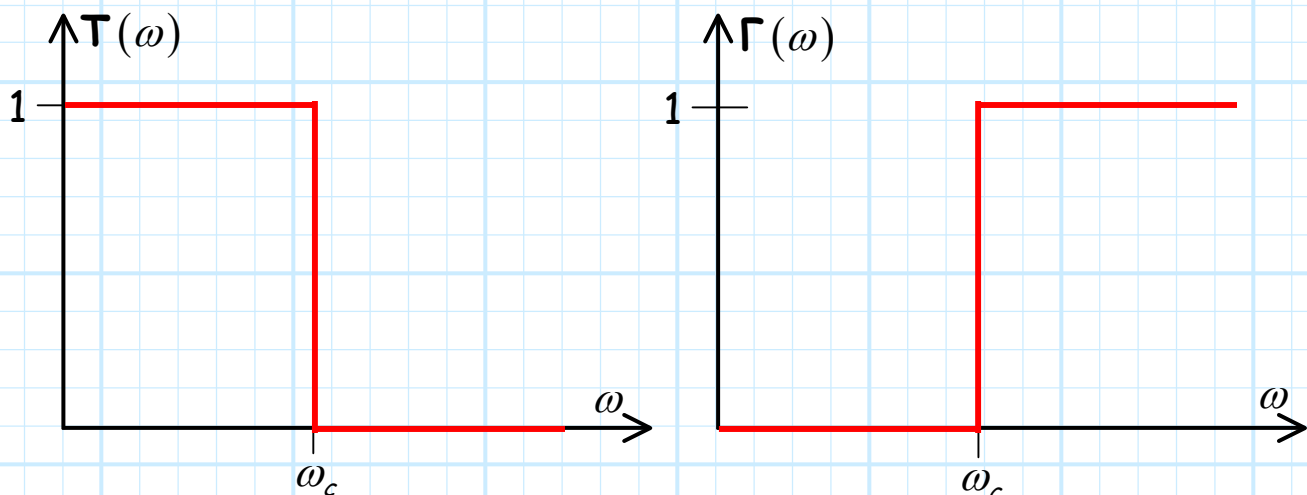
Recall that a **lossless** filter can be described in terms of either its power transmission coefficient $\mathbf{T}(\omega)$ or its power reflection coefficient $\mathbf{\Gamma}(\omega)$, as the two values are completely **dependent**:

$$\mathbf{\Gamma}(\omega) = 1 - \mathbf{T}(\omega)$$

Ideally, these functions would be quite **simple**:

- 1.** $\mathbf{T}(\omega) = 1$ and $\mathbf{\Gamma}(\omega) = 0$ for **all** frequencies within the **pass-band**.
- 2.** $\mathbf{T}(\omega) = 0$ and $\mathbf{\Gamma}(\omega) = 1$ for **all** frequencies within the **stop-band**.

For example, the **ideal** low-pass filter would be:



Add to this a **linear phase** response, and you have the **perfect** microwave filter!

There's just one small problem with this **perfect** filter → It's **impossible** to build!

Now, if we consider only possible (i.e., **realizable**) filters, we must limit ourselves to filter functions that can be expressed as **finite polynomials** of the form:

$$T(\omega) = \frac{a_0 + a_1 \omega + a_2 \omega^2 + \dots}{b_0 + b_1 \omega + b_2 \omega^2 + \dots + b_N \omega^N}$$

The **order** N of the (denominator) polynomial is likewise the **order** of the filter.

There are many different **types** of polynomials that result in good filter responses, and each type has its own set of **characteristics**.

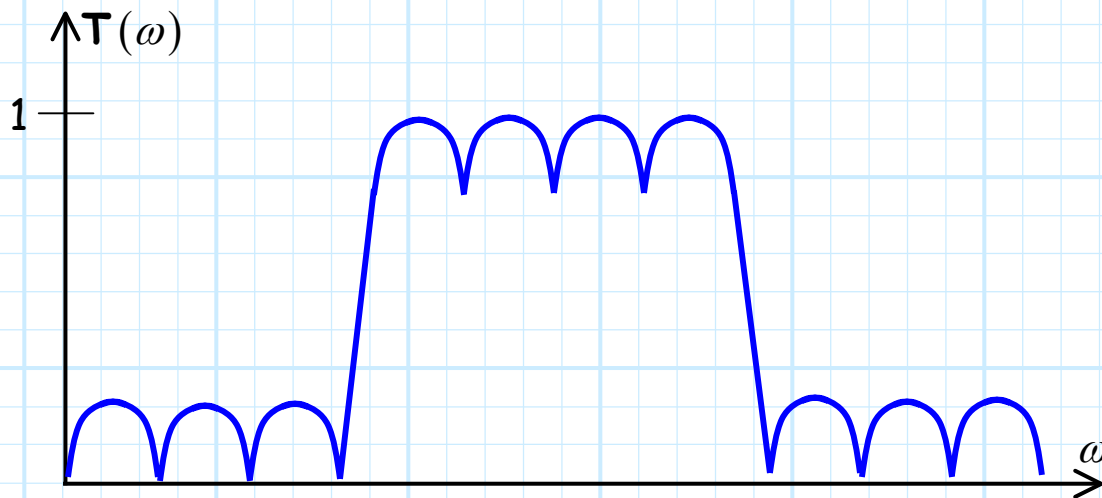
The type of **polynomial** likewise describes the type of microwave **filter**. Let's consider **three** of the most popular types:

1. Elliptical

Elliptical filters have three primary characteristics:

- a) They exhibit very **steep "roll-off"**, meaning that the transition from pass-band to stop-band is very rapid.

- b) They exhibit **ripple** in the **pass-band**, meaning that the value of T will vary slightly within the pass-band.
- c) They exhibit ripple in the **stop-band**, meaning that the value of T will vary slightly within the stop-band.

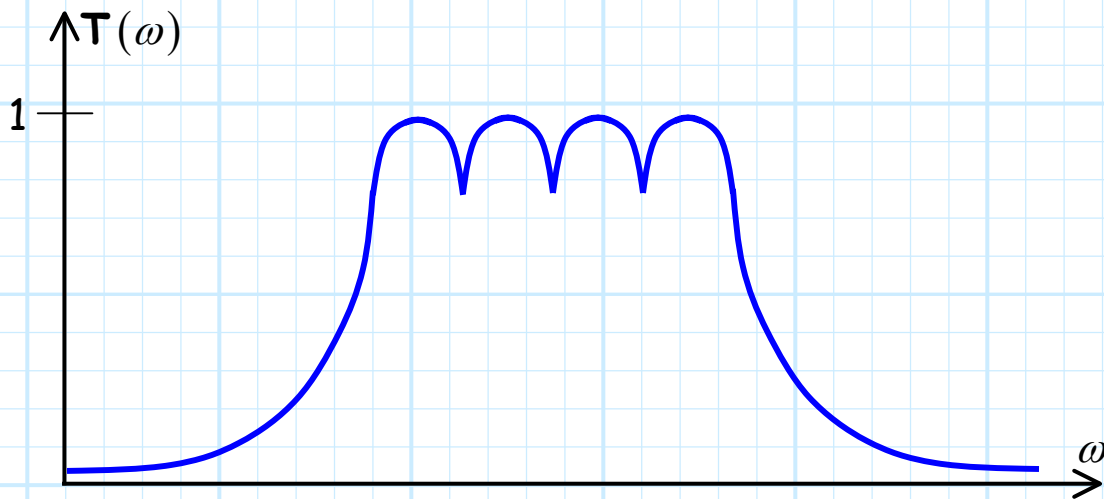


We find that we can make the roll-off **steeper** by accepting more **ripple**.

2. Chebychev

Chebychev filters are also known as **equal-ripple** filters, and have two primary characteristics

- a) **Steep** roll-off (but not as steep as Elliptical).
- b) Pass-band **ripple** (but not stop-band ripple).

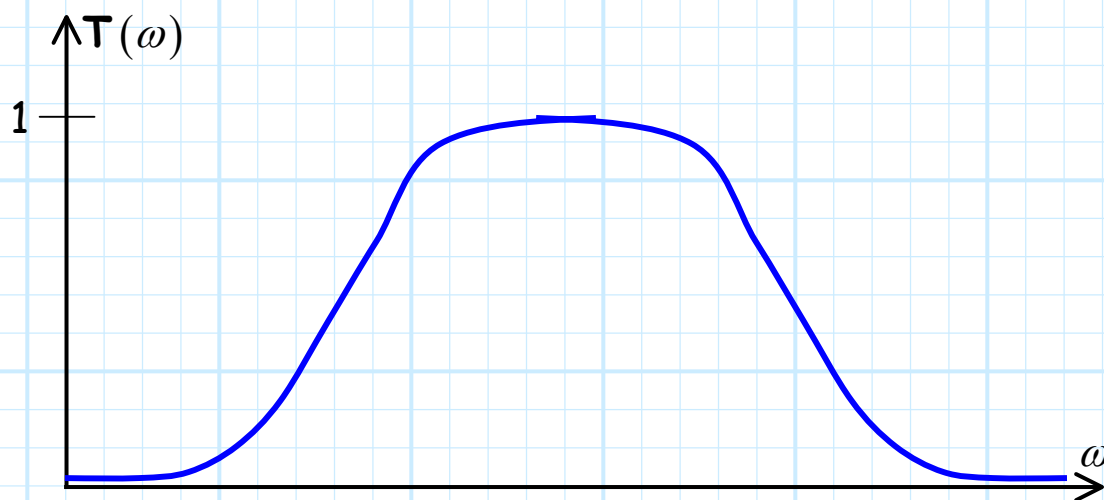


We likewise find that the roll-off can be made steeper by **accepting** more ripple.

3. Butterworth

Also known as **maximally flat filters**, they have two primary characteristics

- a) **Gradual** roll-off .
- b) **No ripple**—not anywhere.



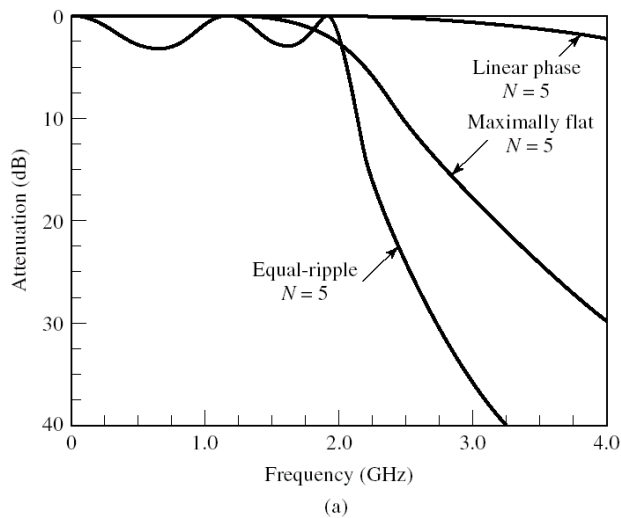
Q: So we always chose *elliptical filters*; since they have the *steepest roll-off*, they are *closest to ideal—right?*

A: Oops! I forgot to talk about the **phase response** $\angle S_{21}(\omega)$ of these filters. Let's examine $\angle S_{21}(\omega)$ for each filter type **before** we pass judgment.

Butterworth $\angle S_{21}(\omega)$ → **Close** to linear phase.

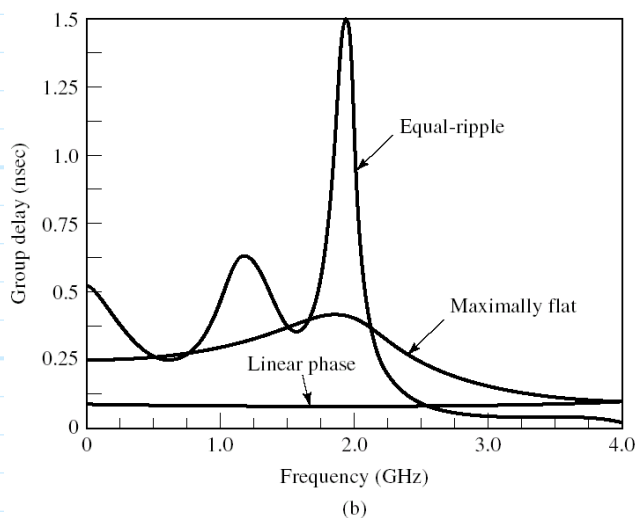
Chebyshev $\angle S_{21}(\omega)$ → **Not** very linear.

Elliptical $\angle S_{21}(\omega)$ → **A big non-linear mess!**



Thus, it is apparent that as a filter roll-off **improves**, the phase response gets **worse** (watch out for **dispersion!**).

→ There is **no** such thing as the "**best**" filter type!



Q: So, a filter with **perfectly linear phase** is impossible to construct?

A: No, it is possible to construct a filter with **near perfect linear phase**—but it will exhibit a **horribly poor roll-off!**

Now, for any **type** of filter, we can **improve** roll-off (i.e., increase stop-band attenuation) by **increasing the filter order N** . However, be aware that increasing the filter order likewise has these **deleterious** effects:

1. It makes **phase response** $\angle S_{21}(\omega)$ worse (i.e., more non-linear).
2. It increases filter **cost, weight, and size**.
3. It increases filter **insertion loss** (this is bad).
4. It makes filter performance more **sensitive** to temperature, aging, etc.

From a **practical** viewpoint, the **order** of a filter should typically be kept to $N < 10$.

Q: *So exactly what **are** these filter polynomials $T(\omega)$? How do we **determine** them?*

A: Fortunately, **radio engineers** do not need to determine specific filter polynomials in order to **specify** (to filter manufacturers) what they want built.

Instead, radio engineers simply can specify the **type** and **order** of a filter, saying things like:

or *"I need a 3^d-order Chebychev filter!"*

or *"Get me a 5th-order Butterworth filter!"*

*"I wish I'd paid **more** attention in EECS 622!"*

Thus, the most **important** filter specifications are:

1. Filter bandwidth and center frequency
2. Filter type and order.

However, there are **many more** important filter specifications!