

PIN Diodes

Q: Just how do we make switches and voltage controlled attenuators?

A: Typically, they are constructed with PIN diodes.

A PIN diode is simply a *p-n* junction diode that is designed to have a very small junction capacitance (0.01 to 0.1 pf).

→ Sort of the opposite of the varactor diode!

To see why this is important, recall diode small signal analysis from your first electronics course.

In small signal analysis, the total diode voltage consists of a D.C. bias voltage (V_D) and a small, time-varying signal (v_d):

$$v_D(t) = V_D + v_d(t)$$

For radio engineering applications, the small signal is a microwave signal !!! I.E.,:

$$v_D(t) = V_D + v_{RF}(t)$$

Thus, we know that the diode current i_D is:

$$i_D = I_s \left(\exp \left[\frac{V_D + v_{RF}(t)}{nV_T} \right] - 1 \right)$$

Since v_{RF} is very small, we can approximate this diode current $i_D(v_D)$ using a **Taylor Series** expansion around $v_D = V_D$:

$$\begin{aligned} i_D(v_D) &\approx i_D(V_D) \Big|_{v_D=V_D} + \frac{\partial i_D(V_D)}{\partial v_D} \Big|_{v_D=V_D} v_{RF}(t) \\ &= I_s \left(e^{\frac{V_D}{nV_T}} - 1 \right) + \frac{I_s e^{\frac{V_D}{nV_T}}}{nV_T} v_{RF}(t) \end{aligned}$$

We recognize that:

$$I_s \left(e^{\frac{V_D}{nV_T}} - 1 \right) = \text{D.C. Bias Current} \doteq I_D$$

and thus we can write our **small-signal approximation** as:

$$\begin{aligned} i_D &= I_D + \frac{(I_D + I_s)}{nV_T} v_{RF}(t) \\ &= I_D + \frac{v_{RF}(t)}{r_d} \end{aligned}$$

where we have defined the diode **small-signal resistance** r_d as:

$$r_d = \frac{nV_T}{I_D + I_s}$$

The diode small-signal resistance is also often referred to as the **junction resistance** R_j or the **series resistance** R_s .

We can further conclude that the total diode current i_D is the sum of the D.C. bias current I_D , and the small-signal current $i_{RF}(t)$, where:

$$i_{RF}(t) = \frac{V_{RF}(t)}{r_d}$$

→ Just like Ohm's Law!

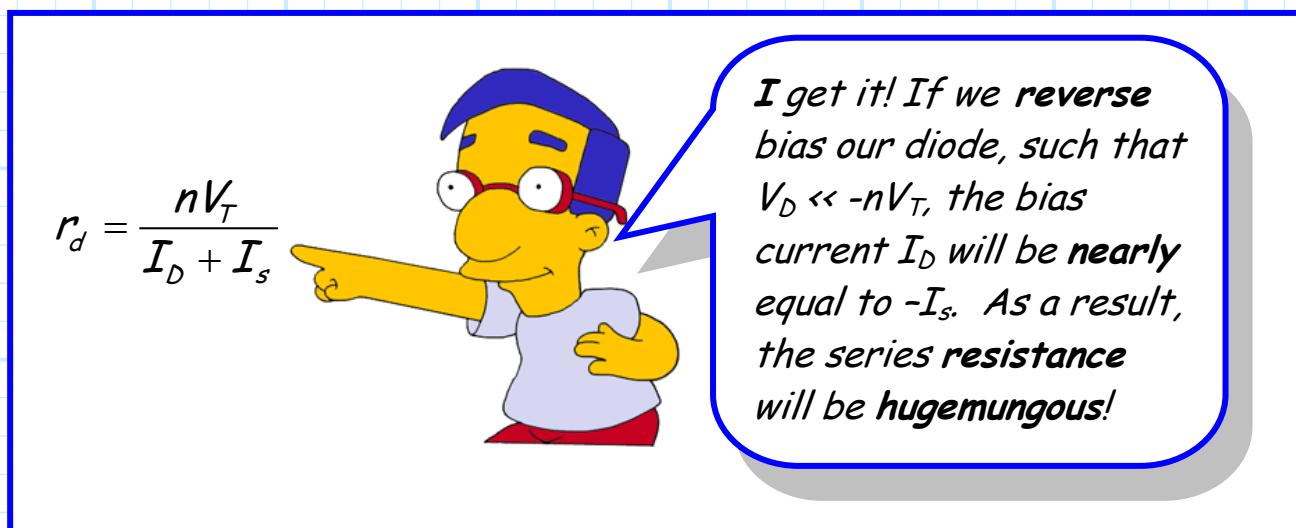
To a small (i.e., low power) microwave signal, a diode "looks" like a resistor.

Moreover, we can control and modify the resistance of the diode by changing the D.C. bias.

→ Sort of a voltage-controlled resistor!

For example, if we put the diode into forward bias ($V_D \gg nV_T$), the bias current I_D will be positive and big, thus the junction resistance will be very small (e.g., r_d = a few ohms).

→ A forward biased diode is very nearly a microwave short circuit!

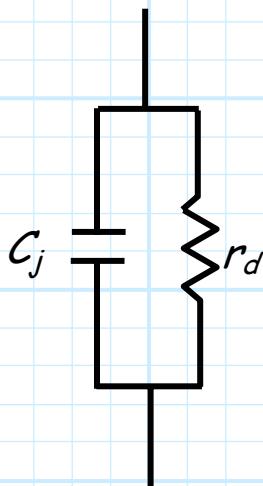


Not so fast! The small-signal **resistance** of a reverse biased diode is in fact **very large**. BUT, we must also consider the junction capacitance C_j !



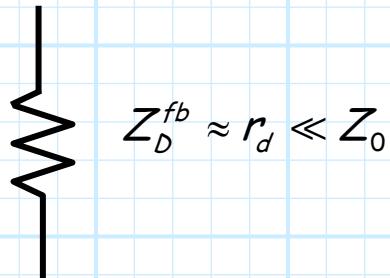
Recall that in **reverse** bias, the junction capacitance of a diode can be **significant**, and in fact generally **increases** as the bias voltage becomes more negative!

As a result, a good microwave circuit **model** of a diode includes both the series resistance and junction capacitance:



$$Z_D = \frac{r_d}{1 + j\omega r_d C_j}$$

For **forward bias**, where r_d is **very small**, we find that diode impedance Z_D is approximately equal to this **small series resistance** ($Z_D \approx r_d$)—a short circuit (approximately):



$$Z_D^{fb} \approx r_d \ll Z_0$$

For reverse bias, where r_d is **very large**, we find that diode impedance Z_D is approximately equal to that of the junction capacitance C_j :

$$\boxed{\frac{1}{j\omega C_j}} \quad Z_D^{rb} = \frac{1}{j\omega C_j} \gg Z_0$$

For low-frequencies (e.g., kHz), this impedance will be typically be **very large** and thus the diode can be approximate as an **open circuit**.

However, at microwave frequencies (where ω is very large) the reverse bias impedance Z_D^{rb} may **not** be particularly large, and thus the reverse biased diode **cannot** be considered an open circuit.

In order for the impedance $Z_D^{rb} = 1/j\omega C_j$ to be **very large** at microwave frequencies, the junction capacitance C_j must be **very, very small**.



PIN diodes! I bet that's why we use PIN diodes!

That's **exactly** why! A PIN diode is **approximately** a **(bias) voltage controlled resistor** at microwave frequencies. We can select any value of r_d from a **short** to an **open**.

As a result, we can make **many** interesting devices!