Parallel Rule

Consider the complex equation:

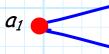
$$b_1 = \alpha a_1 + \beta a_1$$

where α and β are **arbitrary** complex constants. Using the **distributive property**, the equation can equivalently be expressed as:

$$b_1 = (\alpha + \beta) a_1$$

Now let's express these two equations as signal flow graphs!

The first is:



α



 b_1

$$b_1 = \alpha a_1 + \beta a_1$$

With the second:

$$a_1$$

$$\alpha + \beta$$

 $b_1 = (\alpha + \beta) a_1$

Q: Hey wait! If the two equations are **equivalent**, shouldn't the two resulting signal flow graphs **likewise** be equivalent?

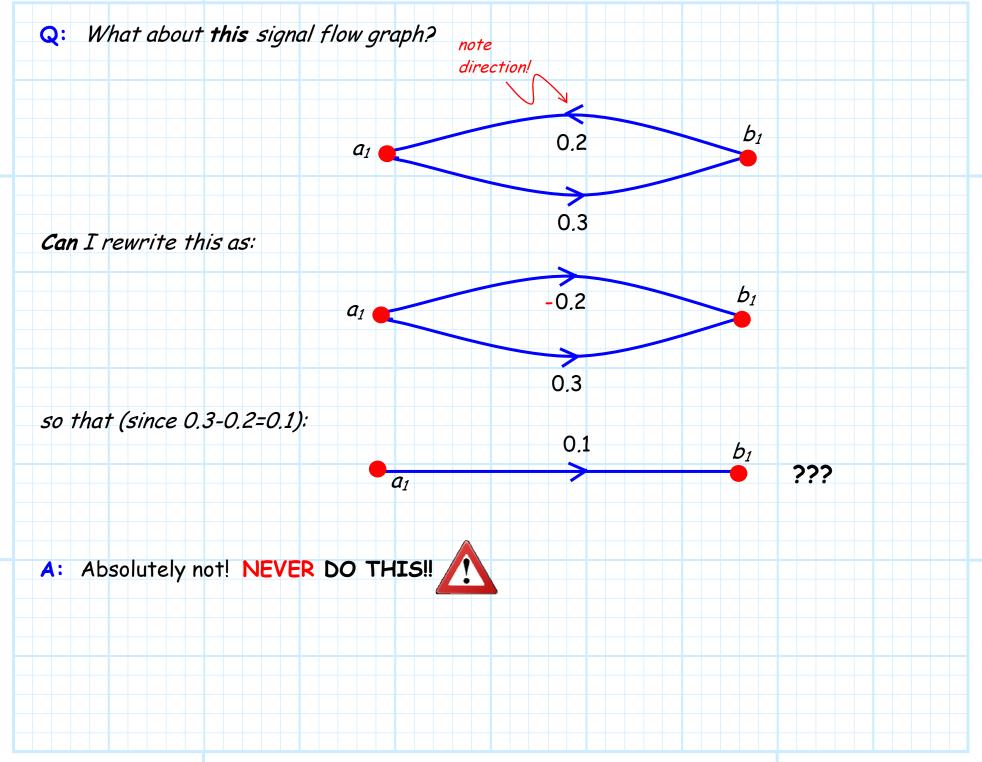
A: Absolutely! The two signal flow graphs are indeed equivalent.

This leads us to our second signal flow graph reduction rule:

Rule 2 - Parallel Rule

If two nodes are connected by parallel branches—and the branches have the same direction—the branches can be combined into a single branch, with a value equal to the sum of each two original branches.

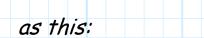
For **example**, the graph: $a_1 = 0.3 a_1 + 0.2 a_1$ 0.3Can be reduced to: $b_1 = 0.3 a_1 + 0.2 a_1$ $b_2 = 0.5 a_1$ 0.5





 a_1

note direction!





$$5 = \frac{1}{0.2}$$



 b_1



0.3

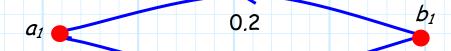


???

A: Absolutely not! NEVER DO THIS EITHER!!



From the signal flow graph below, we can **only** conclude that $b_1 = 0.3 a_1$ and $a_1 = 0.2 b_1$.



0,3

Using the series rule (or little bit of algebra), we can conclude that an equivalent signal flow graph to this is:

$$a_1 = 0.06 a_1$$

 $b_1 = 0.3 a_1$

0.06

 b_1

0.3







A: Branches that begin and end at the same node are called self-loops.

Q: Do these self-loops actually appear in signal flow graphs?

A: Yes, but the self-loop node will always have at least one other incoming branch. For example:

0.06

$$a_1 = 0.06 a_1 - j b_2$$

$$b_1 = 0.3 a_1$$

7-

 b_1

0.3

Q: But how do we reduce a signal flow graph containing a self-loop?

A: See rule 3!