$\stackrel{I_2}{\leftarrow}$

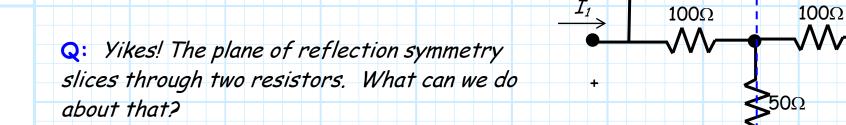
+

V2

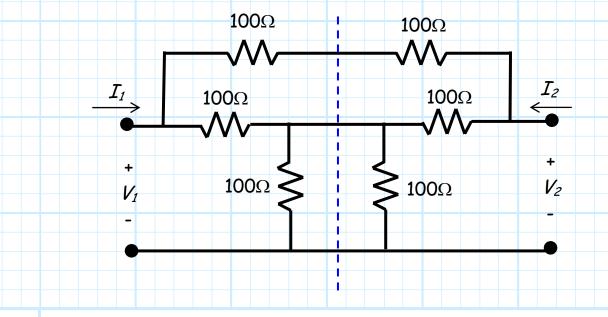
200Ω

Symmetric Circuit Analysis

Consider the following D₁ symmetric **two-port** device:



A: Resistors are easily split into two equal pieces: the 200Ω resistor into two 100Ω resistors in series, and the 50Ω resistor as two 100Ω resistors in parallel.



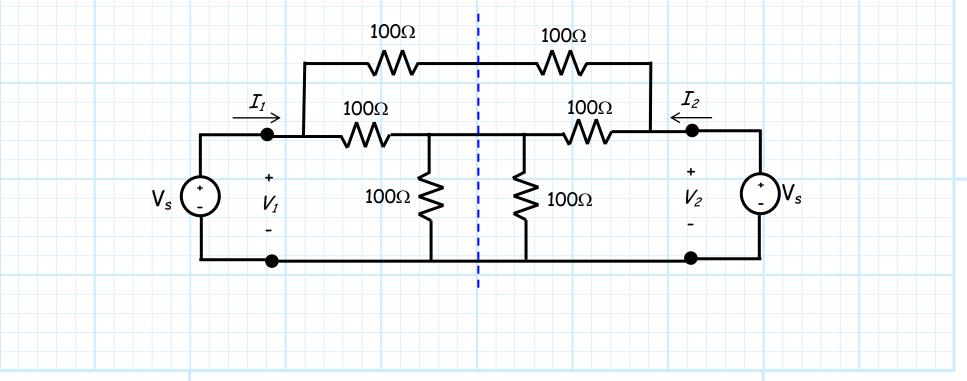
 $S = \begin{vmatrix} S_{11} & S_{21} \\ S_{21} & S_{11} \end{vmatrix} \qquad Z = \begin{vmatrix} Z_{11} & Z_{21} \\ Z_{21} & Z_{11} \end{vmatrix} \qquad Y = \begin{vmatrix} Y_{11} & Y_{21} \\ Y_{21} & Y_{11} \end{vmatrix}$

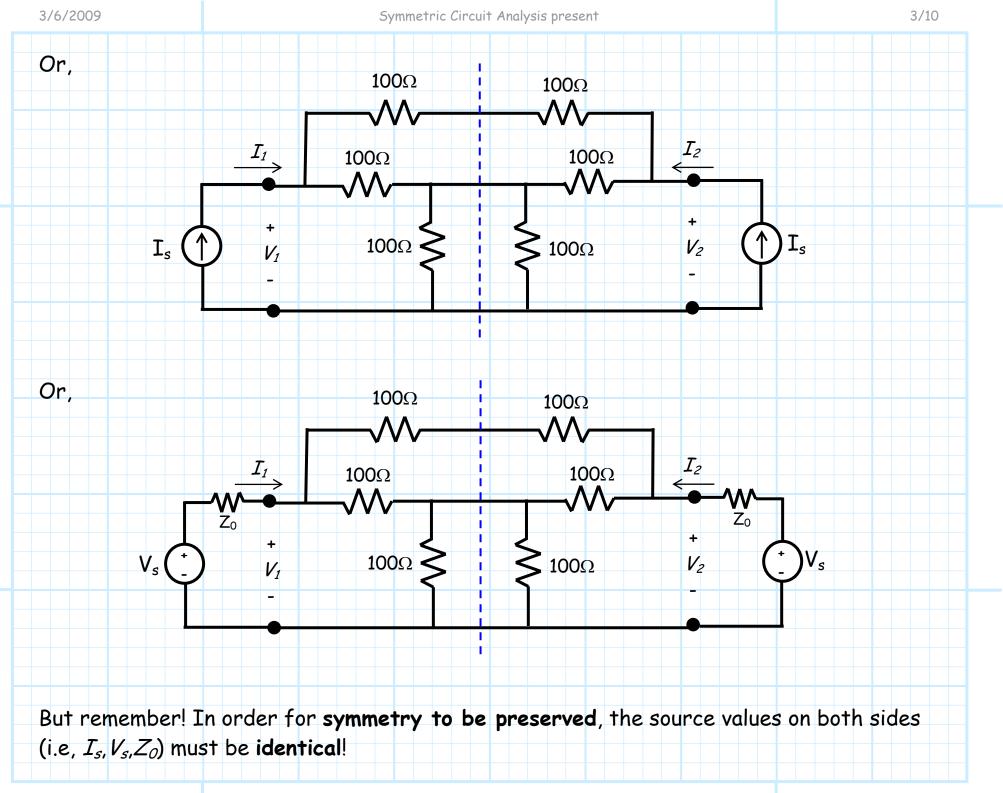
Recall that the symmetry of this 2-port device leads to simplified network matrices:

Q: Yes, but can circuit symmetry likewise simplify the procedure of **determining** these elements? In other words, can symmetry be used to **simplify circuit analysis**?

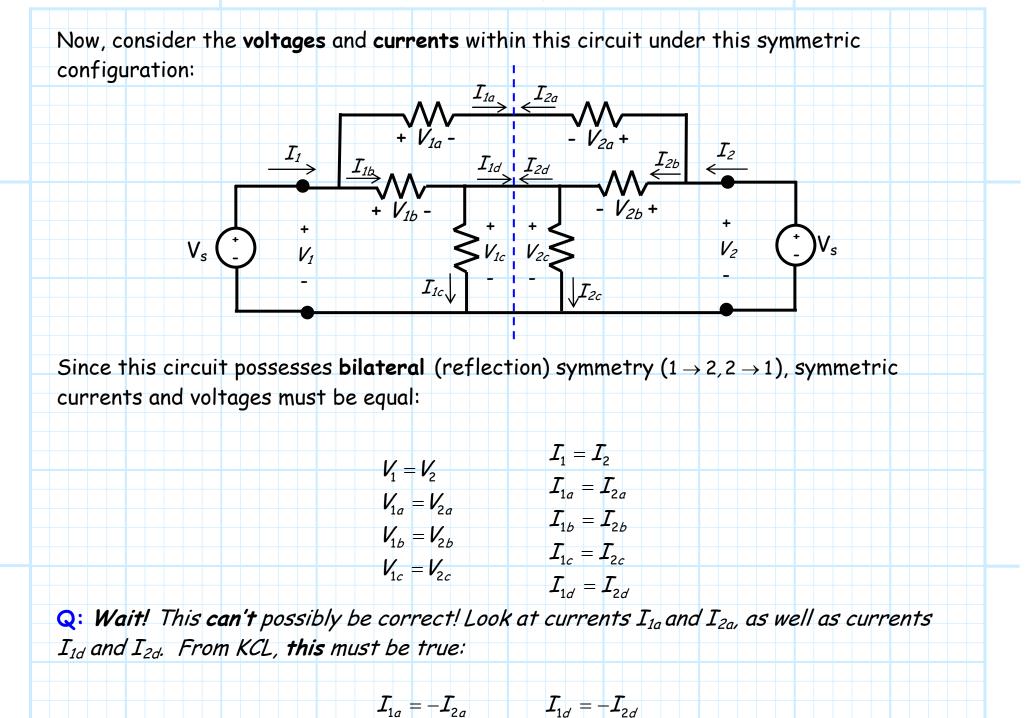
A: You bet!

First, consider the case where we **attach sources** to circuit in a way that **preserves** the circuit **symmetry**:





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Yet you say that this must be true:

$$I_{1a} = I_{2a} \qquad \qquad I_{1d} = I_{2a}$$

There is an **obvious contradiction** here! There is **no way** that both sets of equations can simultaneously be correct, **is there**?

A: Actually there is! There is one solution that will satisfy both sets of equations:

$$I_{1a} = I_{2a} = 0$$
 $I_{1d} = I_{2d} = 0$

The currents are **zero**!

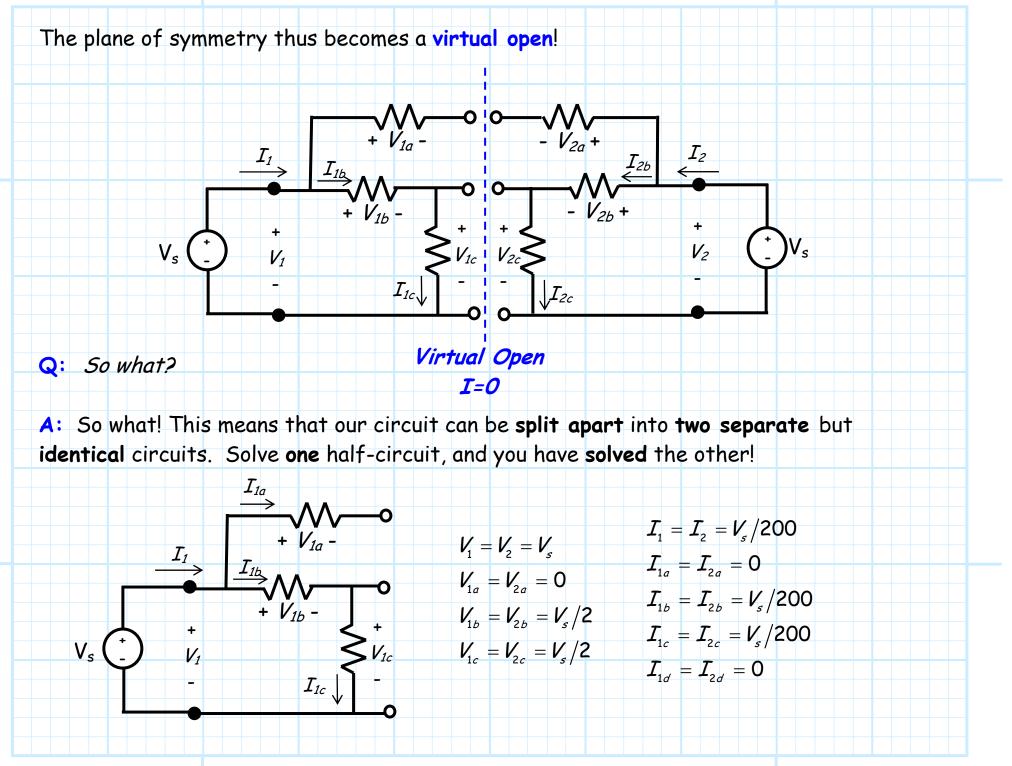


If you **think** about it, this makes **perfect sense**! The result says that **no current** will flow from one side of the symmetric circuit into the other.

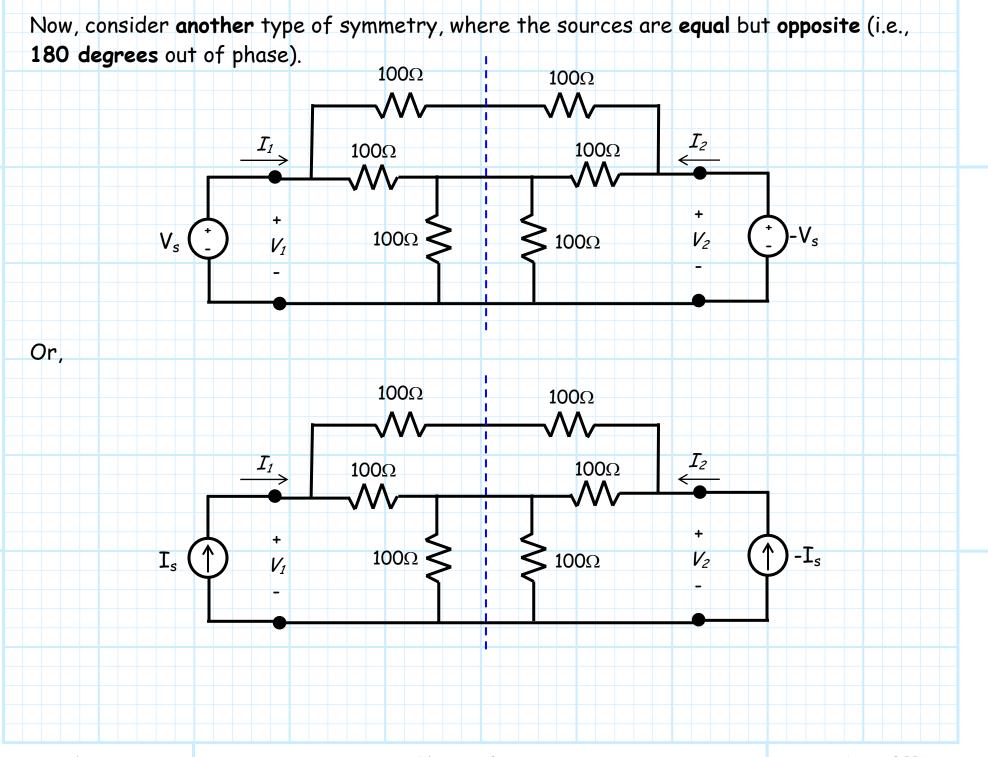
If current did flow across the symmetry plane, then the circuit symmetry would be **destroyed**—one side would effectively become the "source side", and the other the "load side" (i.e., the source side delivers current to the load side).

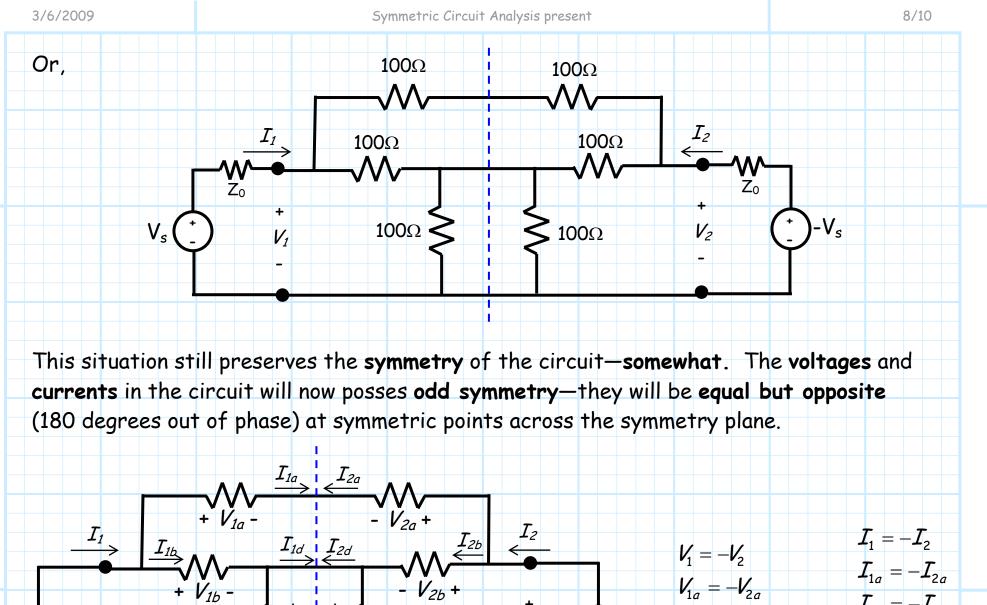
Thus, **no current** will flow **across** the reflection symmetry plane of a **symmetric circuit** the symmetry plane thus acts as a **open circuit**!

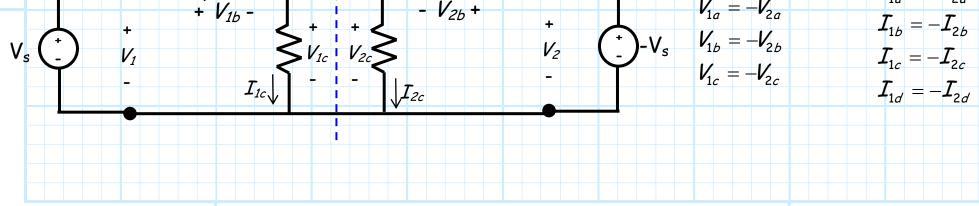
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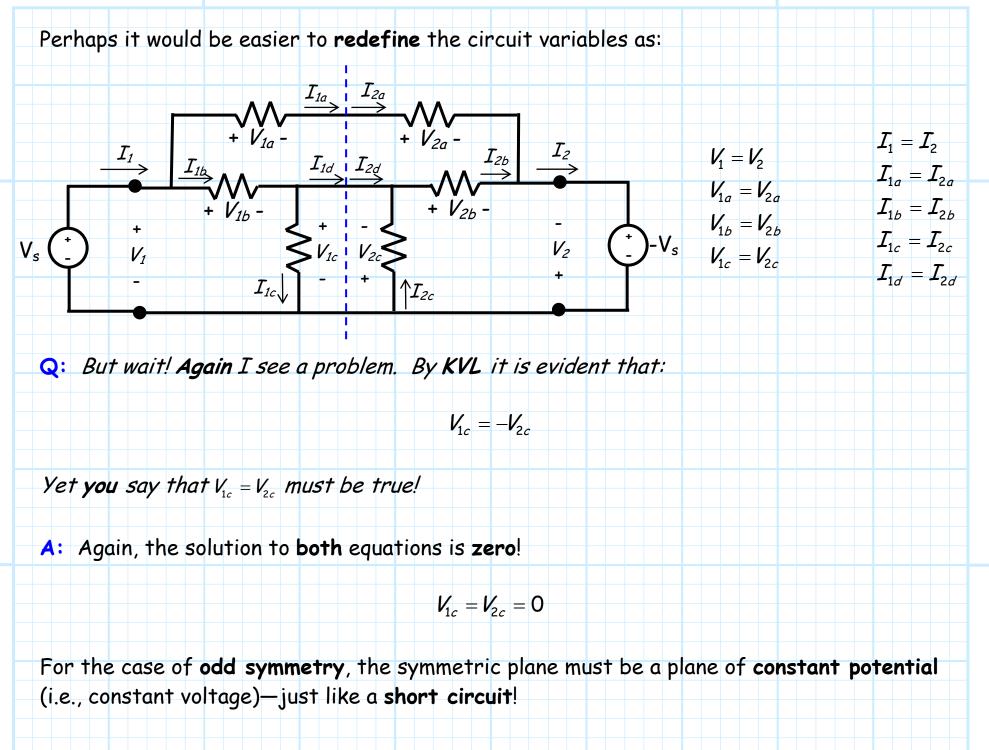












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