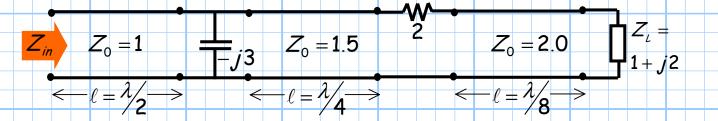
1/5

Example: Input Impedance

Consider the following circuit:



If we **ignored** our new μ -wave knowledge, we might **erroneously** conclude that the input impedance of this circuit is:

$$Z_{in} = -j3$$

Therefore:

$$Z_{in} = \frac{-j3(2+1+j2)}{-j3+2+1+j2} = \frac{6-j9}{3-j} = 2.7 - j2.1$$

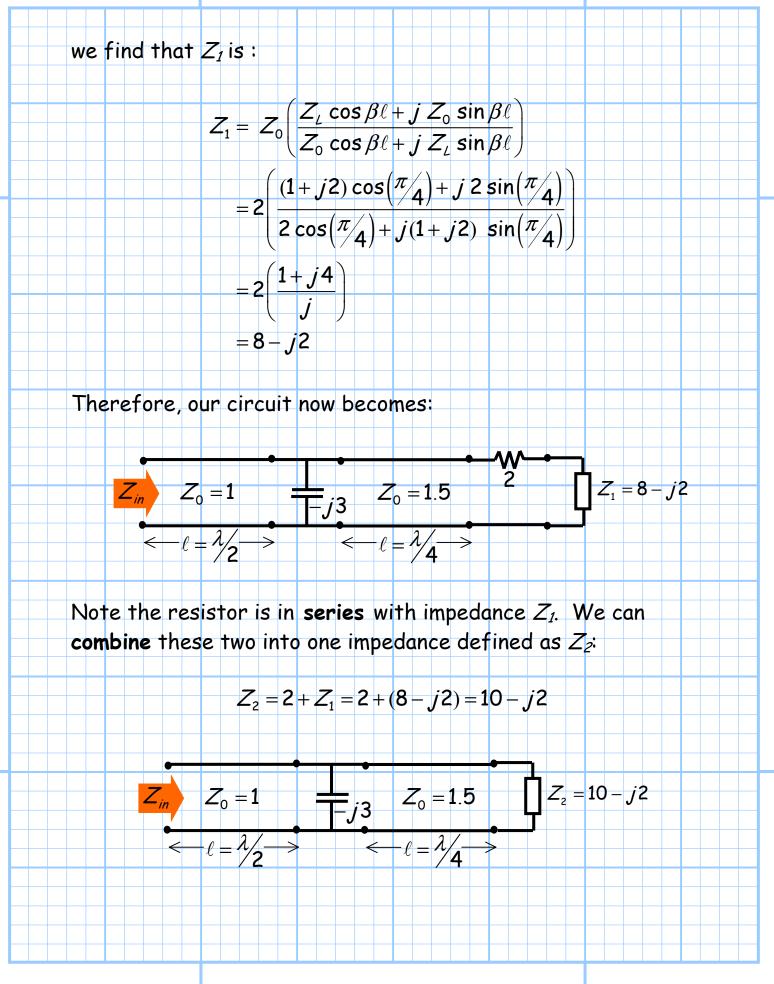
Of course, this is not the correct answer!

We must use our **transmission line theory** to determine an accurate value. Define Z_1 as the input impedance of the last section:

$$Z_0 = 2.0$$

$$Z_1 = 1 + jz$$

$$\zeta_1 = \lambda / z$$

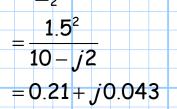


Now let's define the input impedance of the **middle** transmission line section as Z_3 :

$$Z_{3} \qquad Z_{0} = 1.5 \qquad \qquad Z_{2} = 10 - j2$$

$$< \ell = \lambda/ \rightarrow >$$

Note that this transmission line is a **quarter wavelength** $(\ell = \frac{\lambda}{4})$. This is one of the **special** cases we considered earlier! The input impedance Z_3 is:



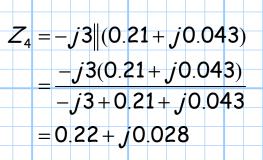
Thus, we can further simplify the original circuit as:

 $\leftarrow \ell = \frac{\lambda}{2}$

 $Z_3 = \frac{Z_0^2}{Z_L}$ $= \frac{Z_0^2}{Z_2}$

$$Z_{in}$$
 $Z_0 = 1$ $= j_3$ $Z_3 = 0.21 + j0.043$

Now we find that the impedance Z_3 is **parallel** to the capacitor. We can **combine** the two impedances and define the result as impedance Z_4 :



Now we are left with **this** equivalent circuit:

Note that the remaining transmission line section is a **half wavelength**! This is one of the **special** situations we discussed in a previous handout. Recall that the **input** impedance in this case is simply equal to the **load** impedance:

$$Z_{in} = Z_L = Z_4 = 0.22 + j0.028$$

Whew! We are **finally** done. The **input impedance** of the original circuit is:

$$Z_{in} = 0.22 + j0.028$$

