

VSWR

Consider again the **voltage** along a terminated transmission line, as a function of **position** z :

$$V(z) = V_0^+ [e^{-j\beta z} + \Gamma e^{+j\beta z}]$$

Recall this is a **complex** function, the magnitude of which expresses the **magnitude** of the **sinusoidal signal** at position z , while the phase of the complex value represents the relative **phase** of the sinusoidal signal.

Let's look at the **magnitude** only:

$$\begin{aligned} |V(z)| &= |V_0^+| |e^{-j\beta z} + \Gamma e^{+j\beta z}| \\ &= |V_0^+| |e^{-j\beta z}| |1 + \Gamma e^{+j2\beta z}| \\ &= |V_0^+| |1 + \Gamma e^{+j2\beta z}| \end{aligned}$$

ICBST the **largest** value of $|V(z)|$ occurs at the location z where:

$$\Gamma e^{+j2\beta z} = |\Gamma| + j0$$

while the **smallest** value of $|V(z)|$ occurs at the location z where:

$$\Gamma e^{+j2\beta z} = -|\Gamma| + j0$$

As a result we can conclude that:

$$|V(z)|_{\max} = |V_0^+| (1 + |\Gamma|)$$

$$|V(z)|_{\min} = |V_0^+| (1 - |\Gamma|)$$

The ratio of $|V(z)|_{\max}$ to $|V(z)|_{\min}$ is known as the **Voltage Standing Wave Ratio (VSWR)**:

$$VSWR \doteq \frac{|V(z)|_{\max}}{|V(z)|_{\min}} = \frac{1 + |\Gamma|}{1 - |\Gamma|} \quad \therefore \quad 1 \leq VSWR \leq \infty$$

Note if $|\Gamma| = 0$ (i.e., $Z_L = Z_0$), then $VSWR = 1$. We find for this case:

$$|V(z)|_{\max} = |V(z)|_{\min} = |V_0^+|$$

In other words, the voltage magnitude is a **constant** with respect to position z .

Conversely, if $|\Gamma| = 1$ (i.e., $Z_L = jX$), then $VSWR = \infty$. We find for **this** case:

$$|V(z)|_{\min} = 0 \quad \text{and} \quad |V(z)|_{\max} = 2|V_0^+|$$

In other words, the voltage magnitude varies **greatly** with respect to position z .

As with **return loss**, VSWR is dependent on the **magnitude** of Γ (i.e, $|\Gamma|$) **only** !

