

2.7 - Lossy Transmission Lines

Reading Assignment: pp. 79-82

Recall that we have been **approximating** low-loss transmission lines as lossless ($R = G = 0$):

$$\alpha = 0 \qquad \beta = \omega\sqrt{LC}$$

But, **long** low-loss lines require a **better** approximation:

$$\alpha = \frac{1}{2} \left(\frac{R}{Z_0} + GZ_0 \right) \qquad \beta = \omega\sqrt{LC}$$

Now, if we have **really long** transmission lines (e.g., long distance communications), we can apply **no** approximations at all:

$$\alpha = \text{Re}\{\gamma\} \qquad \beta = \text{Im}\{\gamma\}$$

For these **very** long transmission lines, we find that $\beta = \text{Im}\{\gamma\}$ is a **function** of signal **frequency** ω . This results in an extremely serious problem—**signal dispersion**.

HO: The Distortionless Line

The Distortionless Line

Recall that the **phase velocity** v_p (i.e., propagation velocity) of a wave in a transmission line is:

$$v_p = \frac{\omega}{\beta}$$

where:

$$\begin{aligned}\beta &= \text{Im}\{\gamma\} \\ &= \text{Im}\left\{\sqrt{(R + j\omega L)(G + j\omega C)}\right\}\end{aligned}$$

Thus, for a lossy line, the phase velocity v_p is a **function of frequency** ω (i.e., $v_p(\omega)$)—this is **bad!**

- * Any signal that carries significant **information** must have some non-zero **bandwidth**. In other words, the signal energy (as well as the information it carries) is **spread** across many frequencies.
- * If the different frequencies that comprise a signal travel at different velocities, that signal will arrive at the end of a transmission line **distorted**. We call this phenomenon signal **dispersion**.

Dispersion: A matter of distance

Recall for **lossless** lines, however, the phase velocity is **independent** of frequency—no dispersion will occur!

$$v_p = \frac{1}{\sqrt{LC}} \quad [R = 0, G = 0]$$

Of course, a perfectly lossless line is impossible, but we find phase velocity is **approximately** constant if the line is low-loss.

Therefore, dispersion distortion on low-loss lines is **most often** not a problem.

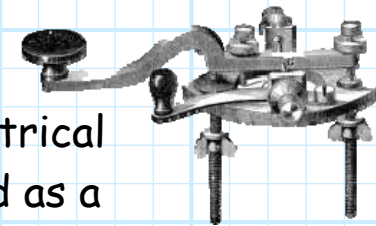
Q: You say "*most often*" not a problem—that phrase seems to imply that dispersion sometimes is a problem!



A: Even for low-loss transmission lines, dispersion can be a problem if the lines are **very** long—just a small difference in phase velocity can result in significant differences in propagation delay if the line is very long!

Purple monkey dishwasher

Modern examples of long transmission lines include phone lines and cable TV. However, the **original** long transmission line problem occurred with the **telegraph**, a device invented and implemented in the 19th century.

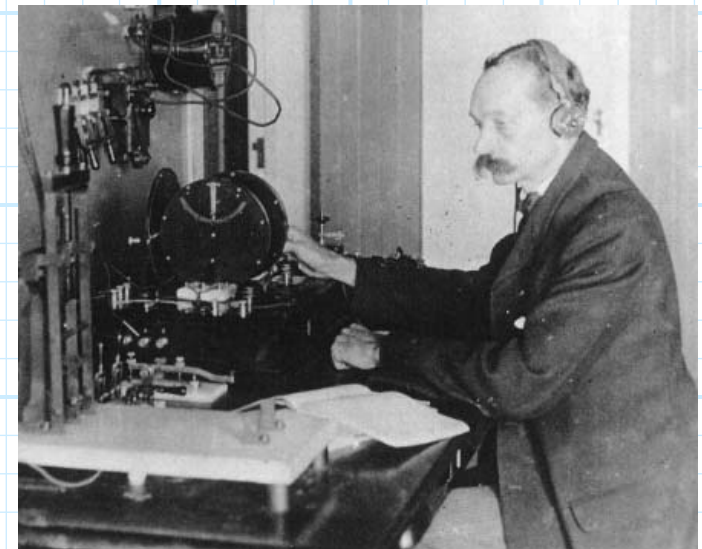


Telegraphy was the essentially the **first** electrical engineering technology ever implemented, and as a result, led to the first ever **electrical engineers!**

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Early telegraph "engineers" discovered that if they made their telegraph lines **too long**, the dots and dashes characterizing Morse code turned into a muddled, indecipherable **mess**. Although they did not realize it, they had fallen victim to the heinous effects of **dispersion!**

Thus, to send messages over long distances, they were forced to implement a series of intermediate "**repeater**" stations, wherein a human operator received and then **retransmitted** a message on to the next station. This **really** slowed things down!

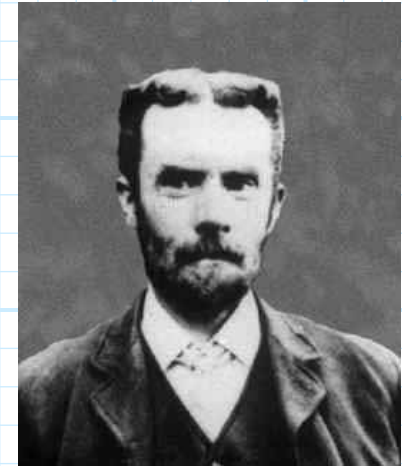


Prevention, not correction!



Q: *Is there any way to prevent dispersion from occurring?*

A: You bet! **Oliver Heaviside** figured out how in the 19th Century!



Heaviside found that a transmission line would be distortionless (i.e., no dispersion) if the line parameters exhibited the following ratio:

$$\frac{R}{L} = \frac{G}{C}$$

Let's see why this works. Note the complex propagation constant γ can be expressed as:

$$\begin{aligned}\gamma &= \sqrt{(R + j\omega L)(G + j\omega C)} \\ &= \sqrt{LC(R/L + j\omega)(G/C + j\omega)}\end{aligned}$$

Then **IF**:

$$\frac{R}{L} = \frac{G}{C}$$

we find:

$$\begin{aligned}\gamma &= \sqrt{LC(R/L + j\omega)(G/C + j\omega)} \\ &= \sqrt{LC(R/L + j\omega)(R/L + j\omega)} \\ &= (R/L + j\omega)\sqrt{LC} \\ &= R\sqrt{\frac{C}{L}} + j\omega\sqrt{LC}\end{aligned}$$

Thus:

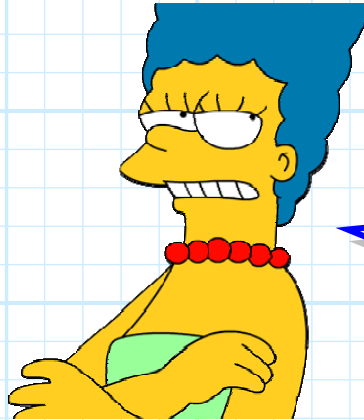
$$\alpha = \text{Re}\{\gamma\} = R\sqrt{\frac{C}{L}} \qquad \beta = \text{Im}\{\gamma\} = \omega\sqrt{LC}$$

The propagation **velocity** of the wave is thus:

$$v_p = \frac{\omega}{\beta} = \frac{1}{\sqrt{LC}} \quad \text{!!!!!!!}$$

The propagation velocity is **independent** of frequency! This lossy transmission line is **not** dispersive!

A Practical implementation



Q: Right. All the transmission lines I use have the property that $R/L > G/C$. I've *never* found a transmission line with this *ideal* property $R/L = G/C$!

A: It is true that typically $R/L > G/C$. But, we can reduce the ratio R/L (until it is equal to G/C) by adding series **inductors** periodically along the transmission line.

This was **Heaviside's** solution—and it worked! **Long** distance transmission lines were made possible.

Q: Why don't we increase G instead?

A: