

## 5.8 - Tapered Lines

**Reading Assignment:** *pp. 255-261*

We can also build matching networks where the characteristic impedance of a transmission line changes **continuously** with position  $z$ .

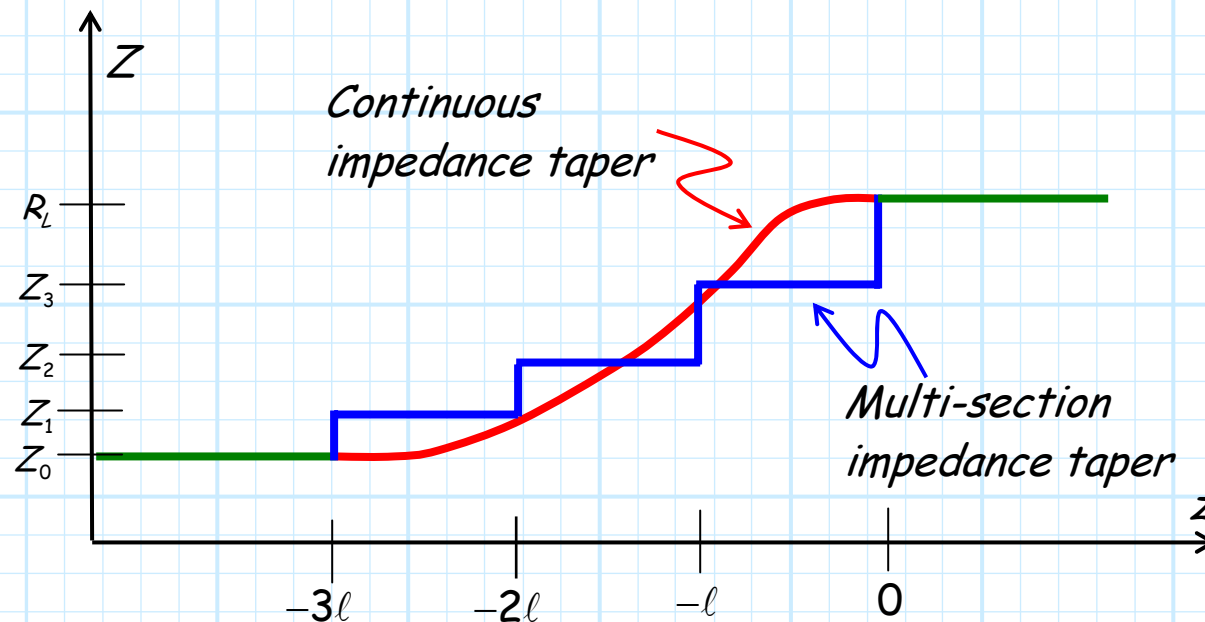
We call these matching networks **tapered lines**.

**HO: TAPERED LINES**

# Tapered Lines

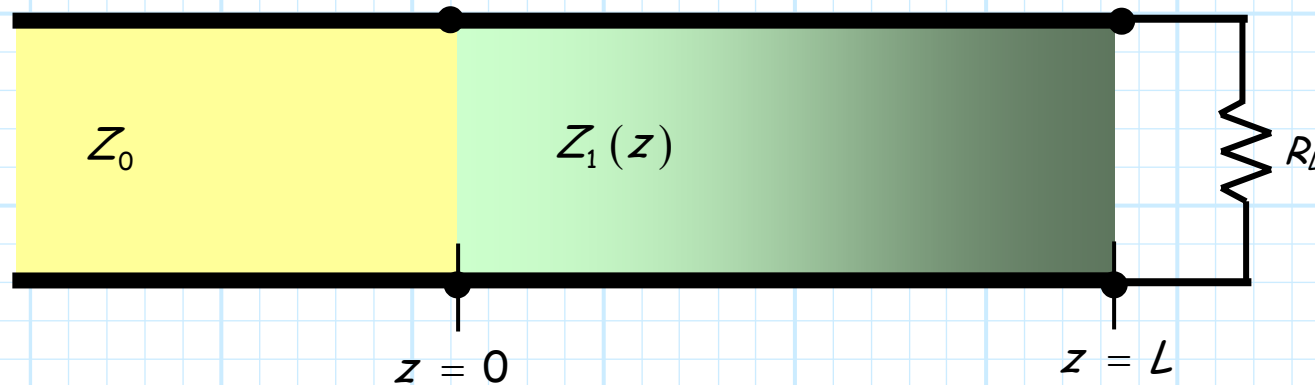
Note **all** our multi-section transformer designs have involved a **monotonic** change in characteristic impedance, from  $Z_0$  to  $R_L$  (e.g.,  $Z_0 < Z_1 < Z_2 < Z_3 < \dots < R_L$ ).

Now, instead of having a **stepped** change in characteristic impedance as a function position  $z$  (i.e., a multi-section transformer), we can also design matching networks with **continuous tapers**.



# Just be glad your name is not Klopfenstein

A tapered impedance matching network is defined by **two** characteristics—its **length**  $L$  and its taper **function**  $Z_1(z)$ :



There are of course an **infinite** number of possible functions  $Z_1(z)$ . Your book discusses **three**: the **exponential** taper, the **triangular** taper, and the **Klopfenstein** taper. For example, the **exponential** taper has the form:

$$Z_1(z) = Z_0 e^{az} \quad 0 < z < L$$

where:

$$a = \frac{1}{L} \ln \left( \frac{Z_L}{Z_0} \right)$$

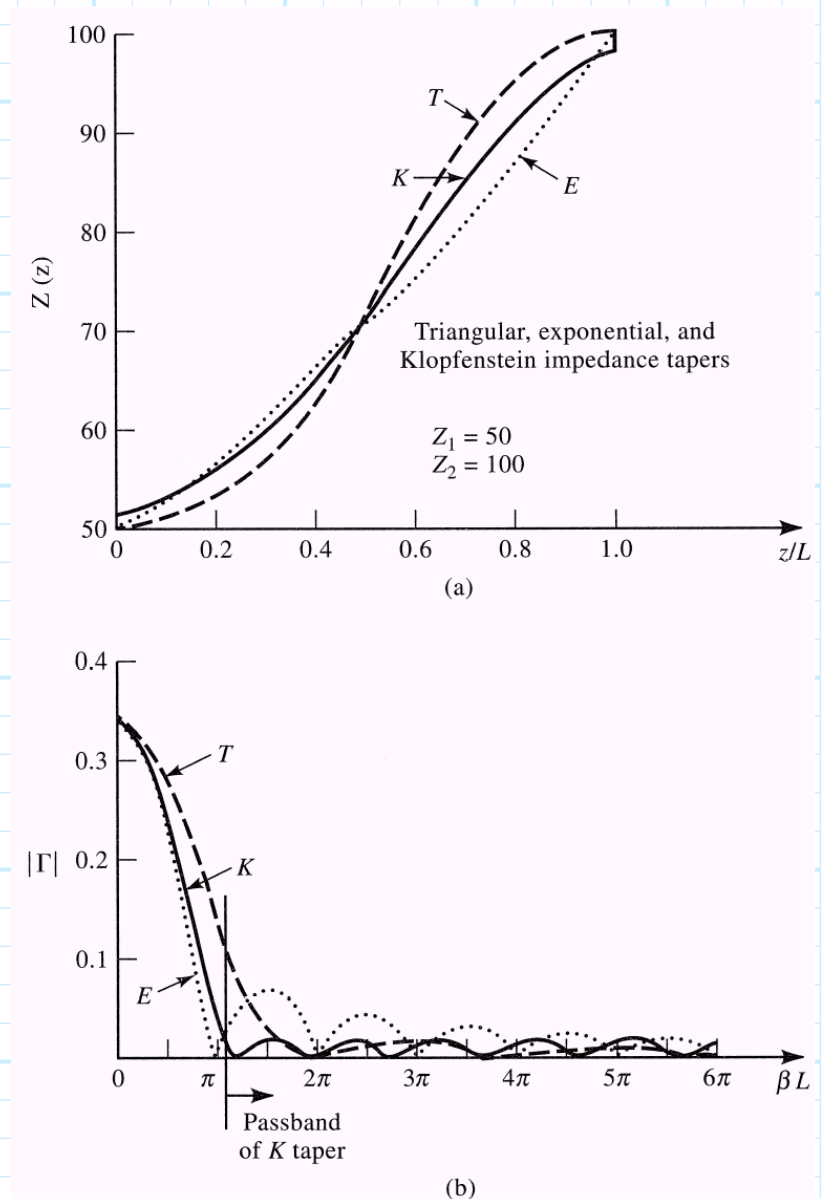
Note for the exponential taper, we get the **expected** result that  $Z_1(z=0) = Z_0$  and  $Z_1(z=L) = R_L$ .

# A longer taper increases bandwidth

Recall the **bandwidth** of a multi-section matching transformer **increases** with the **number** of sections. Similarly, the bandwidth of a tapered line will typically **increase** as the **length**  $L$  is increased.

## Figure 5.21 (p. 260)

*Solution to Example 5.8. (a) Impedance variations for the triangular, exponential, and Klopfenstein tapers. (b) Resulting reflection coefficient magnitude versus frequency for the tapers of (a).*



## Tapers: easily created in microstrip or stripline

**Q:** *But how can we physically taper the characteristic impedance of a transmission line?*

**A:** Most tapered lines are implemented in **stripline** or **microstrip**. As a result, we can modify the characteristic impedance of the transmission line by simply tapering the **width**  $W$  of the conductor (i.e.,  $W(z)$ ).

In other words, we can **continuously** increase or decrease the **width** of the microstrip or stripline to create the **desired** impedance taper  $Z_1(z)$ .