



# Concepts Introduced in Chapter 4

- Grammars
  - Context-Free Grammars
  - Derivations and Parse Trees
  - Ambiguity, Precedence, and Associativity
- Top Down Parsing
  - Recursive Descent, LL
- Bottom Up Parsing
  - SLR, LR, LALR
- Yacc
- Error Handling



# Grammars

$$G = (N, T, P, S)$$

1.  $N$  is a finite set of nonterminal symbols
2.  $T$  is a finite set of terminal symbols
3.  $P$  is a finite subset of

$$(N \cup T)^* N (N \cup T)^* \times (N \cup T)^*$$

An element  $(\alpha, \beta) \in P$  is written as

$$\alpha \rightarrow \beta$$

and is called a production.

4.  $S$  is a distinguished symbol in  $N$  and is called the start symbol.



# Example of a Grammar

*expression*  $\rightarrow$  *expression* + *term*

*expression*  $\rightarrow$  *expression* - *term*

*expression*  $\rightarrow$  *term*

*term*  $\rightarrow$  *term* \* *factor*

*term*  $\rightarrow$  *term* / *factor*

*term*  $\rightarrow$  *factor*

*factor*  $\rightarrow$  ( *expression* )

*factor*  $\rightarrow$  **id**



# Advantages of Using Grammars

- Provides a precise, syntactic specification of a programming language.
- For some classes of grammars, tools exist that can automatically construct an efficient parser.
- These tools can also detect syntactic ambiguities and other problems automatically.
- A compiler based on a grammatical description of a language is more easily maintained and updated.



# Role of a Parser in a Compiler

- Detects and reports any syntax errors.
- Produces a parse tree from which intermediate code can be generated.

*followed by Fig. 4.1*



# Conventions for Specifying Grammars in the Text

- terminals
  - lower case letters early in the alphabet (a, b, c)
  - punctuation and operator symbols [(, ), ', +, −]
  - digits
  - boldface words (**if**, **then**)
- nonterminals
  - uppercase letters early in the alphabet (A, B, C)
  - S is the start symbol
  - lower case words



# Conventions for Specifying Grammars in the Text (cont.)

- grammar symbols (nonterminals or terminals)
  - upper case letters late in the alphabet (X, Y, Z)
- strings of terminals
  - lower case letters late in the alphabet (u, v, ..., z)
- sentential form (string of grammar symbols)
  - lower case Greek letters ( $\alpha$ ,  $\beta$ ,  $\gamma$ )



# Chomsky Hierarchy

A grammar is said to be

1. regular if it is

where each production in  $P$  has the form

a. right-linear

$$A \rightarrow wB \text{ or } A \rightarrow w$$

b. left-linear

$$A \rightarrow Bw \text{ or } A \rightarrow w$$

where  $A, B \in N$  and  $w \in T^*$





# Chomsky Hierarchy (cont)

2. context-free : each production in  $P$  is of the form

$$A \rightarrow \alpha \text{ where } A \in N \text{ and } \alpha \in (N \cup T)^*$$

3. context-sensitive : each production in  $P$  is of the form

$$\alpha \rightarrow \beta \text{ where } |\alpha| \leq |\beta|$$

4. unrestricted if each production in  $P$  is of the form

$$\alpha \rightarrow \beta \text{ where } \alpha \neq \varepsilon$$



# Derivation

- Derivation
  - a sequence of replacements from the start symbol in a grammar by applying productions
    - $E \rightarrow E + E \mid E * E \mid ( E ) \mid - E \mid \mathbf{id}$
- Derive
  - $- ( \mathbf{id} + \mathbf{id} )$  from the grammar
  - $E \Rightarrow - E \Rightarrow - ( E ) \Rightarrow - ( E + E ) \Rightarrow - ( \mathbf{id} + E ) \Rightarrow - ( \mathbf{id} + \mathbf{id} )$
  - thus E derives  $- ( \mathbf{id} + \mathbf{id} )$   
or  $E \Rightarrow - ( \mathbf{id} + \mathbf{id} )$



# Derivation (cont.)

- Leftmost derivation
  - each step replaces the leftmost nonterminal
  - derive  $\text{id} + \text{id} * \text{id}$  using leftmost derivation
    - $E \Rightarrow E + E \Rightarrow \text{id} + E \Rightarrow \text{id} + E * E \Rightarrow$   
 $\text{id} + \text{id} * E \Rightarrow \text{id} + \text{id} * \text{id}$
- $L(G)$  - language generated by the grammar  $G$
- Sentence of  $G$ 
  - if  $S \Rightarrow^+ w$ , where  $w$  is a string of terminals in  $L(G)$
- Sentential form
  - if  $S \Rightarrow^* \alpha$ , where  $\alpha$  may contain nonterminals

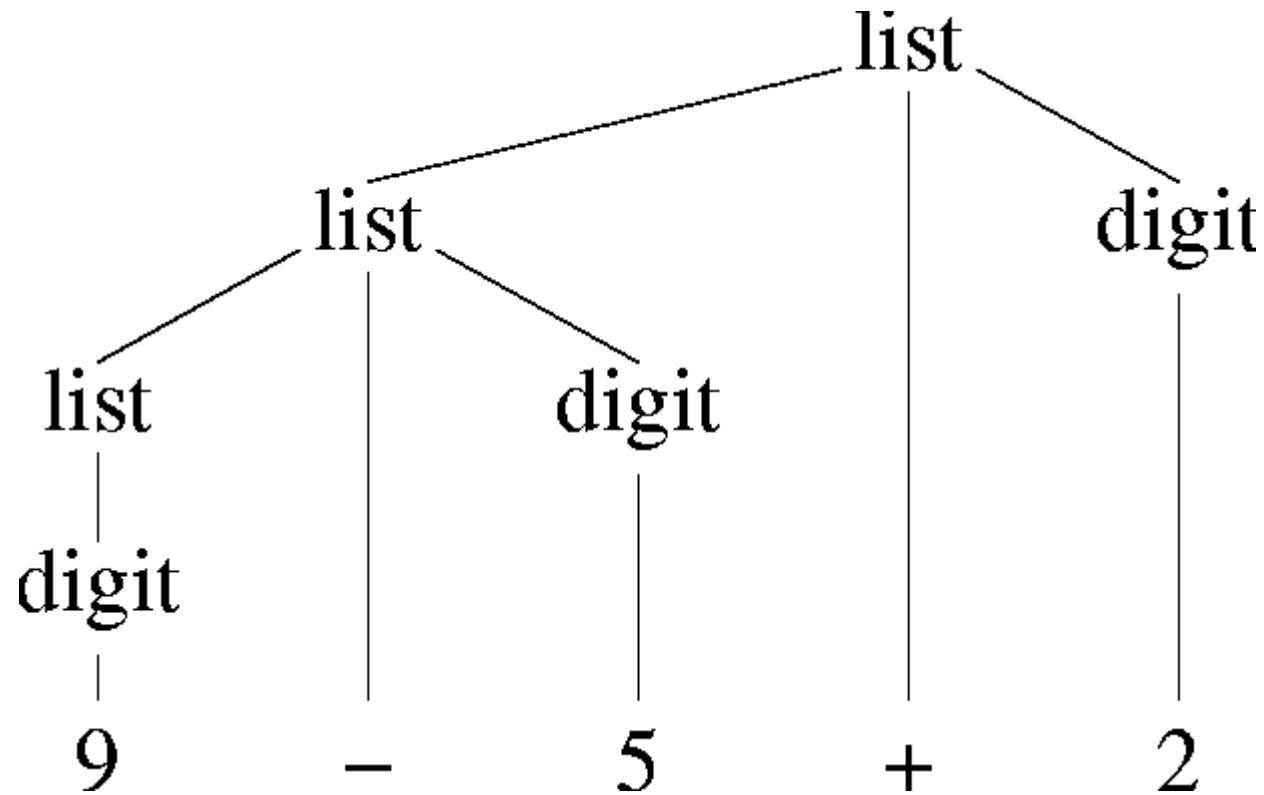


# Parse Tree

- Parse tree pictorially shows how the start symbol of a grammar derives a specific string in the language.
- Given a context-free grammar, a parse tree has the properties:
  - The root is labeled by the start symbol.
  - Each leaf is labeled by a token or  $\epsilon$ .
  - Each interior node is labeled by a nonterminal.
  - If  $A$  is a nonterminal labeling some interior node and  $X_1, X_2, X_3, \dots, X_n$  are the labels of the children of that node from left to right, then  
 $A \rightarrow X_1, X_2, X_3, \dots, X_n$  is a production of the grammar.



# Example of a Parse Tree



$\text{list} \rightarrow \text{list} + \text{digit} \mid \text{list} - \text{digit} \mid \text{digit}$

*followed by Fig. 4.4*



# Parse Tree (cont.)

- Yield
  - the leaves of the parse tree read from left to right, or
  - the string derived from the nonterminal at the root of the parse tree
- An ambiguous grammar is one that can generate two or more parse trees that yield the same string.

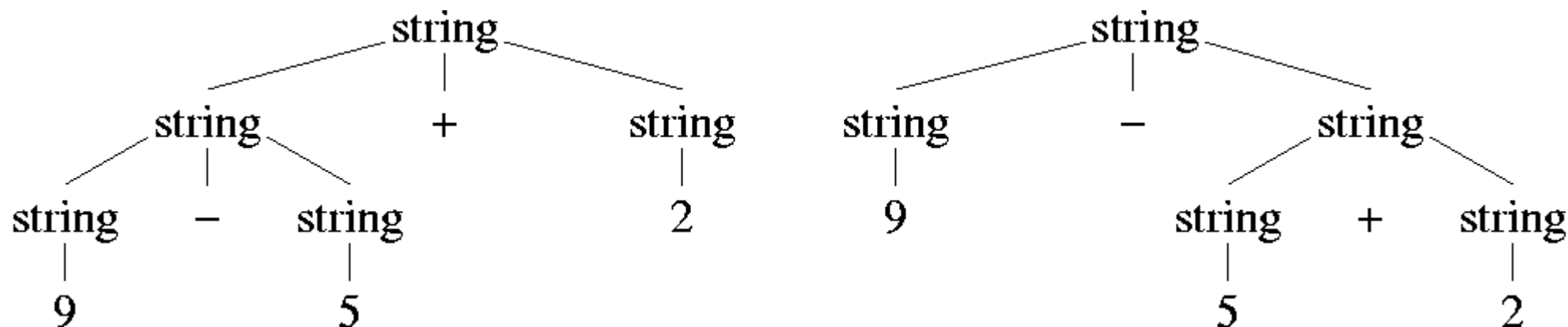


# Example of an Ambiguous Grammar

string  $\rightarrow$  string + string

string  $\rightarrow$  string - string

string  $\rightarrow$  0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9



a. string  $\rightarrow$  string + string  $\rightarrow$  string - string + string  
 $\rightarrow$  9 - string + string  $\rightarrow$  9 - 5 + string  $\rightarrow$  9 - 5 + 2

b. string  $\rightarrow$  string - string  $\rightarrow$  9 - string  
 $\rightarrow$  9 - string + string  $\rightarrow$  9 - 5 + string  $\rightarrow$  9 - 5 + 2

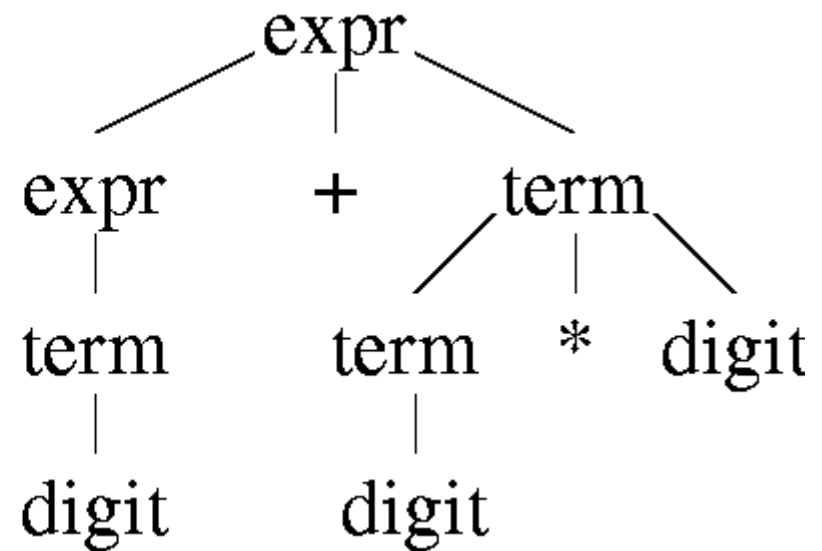


# Precedence

By convention

$9 + 5 * 2$        $*$  has higher precedence than  $+$  because  
it takes its operands before  $+$

$\text{expr} \rightarrow \text{expr} + \text{term} \mid \text{term}$   
 $\text{term} \rightarrow \text{term} * \text{digit} \mid \text{digit}$







## Precedence (cont.)

- If different operators have the same precedence then they are defined as alternative productions of the same nonterminal.

$$\text{expr} \rightarrow \text{expr} + \text{term} \mid \text{expr} - \text{term} \mid \text{term}$$
$$\text{term} \rightarrow \text{term} * \text{factor} \mid \text{term} / \text{factor} \mid \text{factor}$$
$$\text{factor} \rightarrow \text{digit} \mid (\text{expr})$$



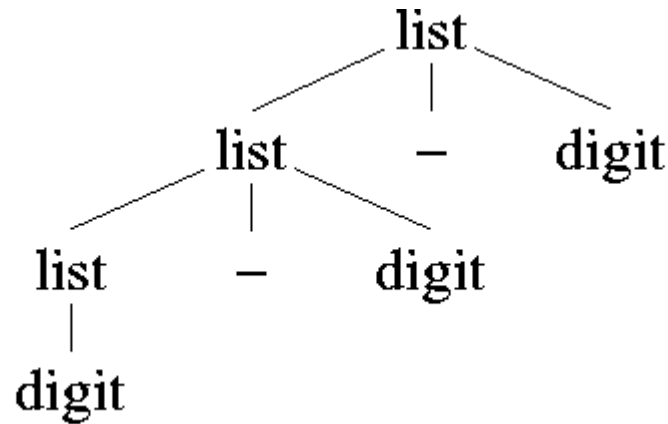
# Associativity

By convention

$9 - 5 - 2$  left (operand with  $-$  on both sides is taken by the operator to its left)

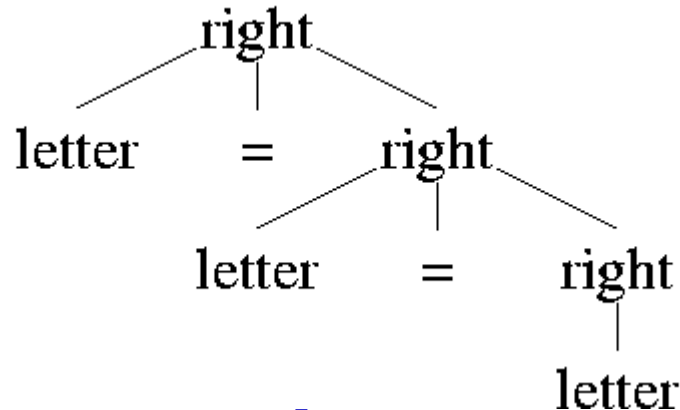
$a = b = c$  right

$\text{list} \rightarrow \text{list} - \text{digit}$   
 $\text{list} \rightarrow \text{digit}$



grows to the left

$\text{right} \rightarrow \text{letter} = \text{right}$   
 $\text{right} \rightarrow \text{letter}$



grows to the right



# Eliminating Ambiguity

- Sometimes ambiguity can be eliminated by rewriting a grammar.
- $\text{stmt} \rightarrow$  **if** expr **then** stmt  
                  |   **if** expr **then** stmt **else** stmt  
                  |   other
- How do we parse:  
**if** E1 **then** **if** E2 **then** S1 **else** S2

*followed by Fig. 4.9*



# Eliminating Ambiguity (cont.)

- $\text{stmt} \rightarrow \begin{array}{l} \text{matched\_stmt} \\ | \\ \text{unmatched\_stmt} \end{array}$
- $\text{matched\_stmt} \rightarrow \begin{array}{l} \text{if expr then matched\_stmt else matched\_stmt} \\ | \\ \text{other} \end{array}$
- $\text{unmatched\_stmt} \rightarrow \begin{array}{l} \text{if expr then stmt} \\ | \\ \text{if expr then matched\_stmt else unmatched\_stmt} \end{array}$



# Parsing

- Universal
- Top-down
  - recursive descent
  - LL
- Bottom-up
  - LR
    - SLR
    - canonical LR
    - LALR



# Top-Down vs Bottom-Up Parsing

- top-down
  - Have to eliminate left recursion in the grammar.
  - Have to left factor the grammar.
  - Resulting grammars are harder to read and understand.
- bottom-up
  - Difficult to implement by hand, so a tool is needed.



# Top-Down Parsing

Starts at the root and proceeds towards the leaves.

Recursive-Descent Parsing - a recursive procedure is associated with each nonterminal in the grammar.

## Example

- $\text{type} \rightarrow \text{simple} \mid \uparrow \underline{\text{id}} \mid \underline{\text{array}} \text{ [ simple ] } \underline{\text{of}} \text{ type}$
- $\text{simple} \rightarrow \underline{\text{integer}} \mid \underline{\text{char}} \mid \underline{\text{num}} \underline{\text{dotdot}} \underline{\text{num}}$

*followed by Fig. 4.12*



# Example of Recursive Descent Parsing

```
void type() {  
    if ( lookahead == INTEGER || lookahead == CHAR ||  
        lookahead == NUM)  
        simple();  
    else if (lookahead == '^') {  
        match('^');  
        match(ID);  
    }  
    else if (lookahead == ARRAY) {  
        match(ARRAY);  
        match '[';  
        simple();  
        match ']';  
        match(OF);  
        type();  
    }  
    else  
        error();  
}
```





# Example of Recursive Descent Parsing (cont.)

```
void simple() {  
    if (lookahead == INTEGER)  
        match(INTEGER);  
    else if (lookahead == CHAR)  
        match(CHAR);  
    else if (lookahead == NUM) {  
        match(NUM);  
        match(DOTDOT);  
        match(NUM);  
    }  
    else  
        error();  
}
```

```
void match(token t)  
{  
    if (lookahead == t)  
        lookahead = nexttoken();  
    else  
        error();  
}
```



# Top-Down Parsing (cont.)

- Predictive parsing needs to know what first symbols can be generated by the right side of a production.
- $\text{FIRST}(\alpha)$  - the set of tokens that appear as the first symbols of one or more strings generated from  $\alpha$ . If  $\alpha$  is  $\epsilon$  or can generate  $\epsilon$ , then  $\epsilon$  is also in  $\text{FIRST}(\alpha)$ .
- Given a production

$$A \rightarrow \alpha \mid \beta$$

predictive parsing requires  $\text{FIRST}(\alpha)$  and  $\text{FIRST}(\beta)$  to be disjoint.



# Eliminating Left Recursion

- Recursive descent parsing loops forever on left recursion.
- Immediate Left Recursion

Replace  $A \rightarrow A\alpha \mid \beta$  with  $A \rightarrow \beta A'$   
 $A' \rightarrow \alpha A' \mid \epsilon$

Example:

|                                    | <u>A</u> | <u><math>\alpha</math></u> | <u><math>\beta</math></u> |
|------------------------------------|----------|----------------------------|---------------------------|
| $E \rightarrow E + T \mid T$       | E        | +T                         | T                         |
| $T \rightarrow T * F \mid F$       | T        | *F                         | F                         |
| $F \rightarrow (E) \mid \text{id}$ |          |                            |                           |

becomes

$$\begin{aligned} E &\rightarrow TE' \\ E' &\rightarrow +TE' \mid \epsilon \\ T &\rightarrow FT' \end{aligned}$$



# Eliminating Left Recursion (cont.)

In general, to eliminate left recursion given  $A_1, A_2, \dots, A_n$

```
for i = 1 to n do {  
  for j = 1 to i-1 do {  
    replace each  $A_i \rightarrow A_j \gamma$  with  $A_i \rightarrow \delta_1 \gamma \mid \dots \mid \delta_k \gamma$   
    where  $A_j \rightarrow \delta_1 \mid \delta_2 \mid \dots \mid \delta_k$  are the current  $A_j$   
    productions  
  }  
  eliminate immediate left recursion in  $A_i$  productions  
  eliminate  $\epsilon$  transitions in the  $A_i$  productions  
}
```

This fails only if cycles ( $A \Rightarrow^+ A$ ) or  $A \rightarrow \epsilon$  for some  $A$ .



# Example of Eliminating Left Recursion

1.  $X \rightarrow YZ \mid a$
2.  $Y \rightarrow ZX \mid Xb$
3.  $Z \rightarrow XY \mid ZZ \mid a$

$$A1 = X \quad A2 = Y \quad A3 = Z$$

$i = 1$  (eliminate immediate left recursion)  
nothing to do



# Example of Eliminating Left Recursion (cont.)

$i = 2, j = 1$

$Y \rightarrow Xb \Rightarrow Y \rightarrow ZX \mid YZb \mid ab$

now eliminate immediate left recursion

$Y \rightarrow ZXY' \mid abY'$

$Y' \rightarrow ZbY' \mid \epsilon$

now eliminate  $\square$  transitions

$Y \rightarrow ZXY' \mid abY' \mid ZX \mid ab$

$Y' \rightarrow ZbY' \mid Zb$

$i = 3, j = 1$

$Z \rightarrow XY \Rightarrow Z \rightarrow YZY \mid aY \mid ZZ \mid a$



# Example of Eliminating Left Recursion (cont.)

$i = 3, j = 2$

$$Z \rightarrow YZY \Rightarrow Z \rightarrow ZXY'ZY \mid ZXZY \mid abY'ZY \\ \mid abZY \mid aY \mid ZZ \mid a$$

now eliminate immediate left recursion

$$Z \rightarrow abY'ZYZ' \mid abZYZ' \mid aYZ' \mid aZ' \\ Z' \rightarrow XY'ZYZ' \mid XZYZ' \mid ZZ' \mid \epsilon$$

eliminate  $\epsilon$  transitions

$$Z \rightarrow abY'ZYZ' \mid abY'ZY \mid abZYZ' \mid abZY \mid aY \\ \mid aYZ' \mid aZ' \mid a \\ Z' \rightarrow XY'ZYZ' \mid XY'ZY \mid XZYZ' \mid XZY \mid ZZ' \mid Z$$



# Left-Factoring

$$A \rightarrow \alpha\beta \mid \alpha\gamma \quad \Rightarrow \quad \begin{array}{l} A \rightarrow \alpha A' \\ A' \rightarrow \beta \mid \gamma \end{array}$$

Example:

Left factor

$$\begin{array}{l} \text{stmt} \rightarrow \underline{\text{if}} \text{ cond } \underline{\text{then}} \text{ stmt } \underline{\text{else}} \text{ stmt} \\ \quad \mid \underline{\text{if}} \text{ cond } \underline{\text{then}} \text{ stmt} \end{array}$$

becomes

$$\begin{array}{l} \text{stmt} \rightarrow \underline{\text{if}} \text{ cond } \underline{\text{then}} \text{ stmt } E \\ E \rightarrow \underline{\text{else}} \text{ stmt } \mid \epsilon \end{array}$$

Useful for predictive parsing since we will know which production to choose.





# Nonrecursive Predictive Parsing

- Instead of recursive descent, it is table-driven and uses an explicit stack. It uses
  1. a stack of grammar symbols (\$ on bottom)
  2. a string of input tokens (\$ on end)
  3. a parsing table [NT, T] of productions

*followed by Fig. 4.19*



# Algorithm for Nonrecursive Predictive Parsing

1. If  $\text{top} == \text{input} == \$$  then accept
2. If  $\text{top} == \text{input}$  then
  - pop top off the stack
  - advance to next input symbol
  - goto 1
3. If top is nonterminal
  - fetch  $M[\text{top}, \text{input}]$
  - If a production
    - replace top with rhs of production
  - Else
    - parse fails
  - goto 1
4. Parse fails

*followed by Fig. 4.17, 4.21*



# First

$\text{FIRST}(\alpha)$  = the set of terminals that begin strings derived from  $\alpha$ . If  $\alpha$  is  $\epsilon$  or generates  $\epsilon$ , then  $\epsilon$  is also in  $\text{FIRST}(\alpha)$ .

1. If  $X$  is a terminal then  $\text{FIRST}(X) = \{X\}$
2. If  $X \rightarrow a\alpha$ , add  $a$  to  $\text{FIRST}(X)$
3. If  $X \rightarrow \epsilon$ , add  $\epsilon$  to  $\text{FIRST}(X)$
4. If  $X \rightarrow Y_1, Y_2, \dots, Y_k$  and  $Y_1, Y_2, \dots, Y_{i-1} \xRightarrow{*} \epsilon$  where  $i \leq k$

Add every non  $\epsilon$  in  $\text{FIRST}(Y_i)$  to  $\text{FIRST}(X)$   
If  $Y_1, Y_2, \dots, Y_k \xRightarrow{*} \epsilon$ , add  $\epsilon$  to  $\text{FIRST}(X)$



# FOLLOW

$\text{FOLLOW}(A)$  = the set of terminals that can immediately follow  $A$  in a sentential form.

1. If  $S$  is the start symbol, add  $\$$  to  $\text{FOLLOW}(S)$
2. If  $A \rightarrow \alpha B \beta$ , add  $\text{FIRST}(\beta) - \{\epsilon\}$  to  $\text{FOLLOW}(B)$
3. If  $A \rightarrow \alpha B$  or  $A \rightarrow \alpha B \beta$  and  $\beta^* \Rightarrow \epsilon$ ,  
add  $\text{FOLLOW}(A)$  to  $\text{FOLLOW}(B)$



# Example of Calculating FIRST and FOLLOW

| Production                          | FIRST               | FOLLOW              |
|-------------------------------------|---------------------|---------------------|
| $E \rightarrow TE'$                 | $\{ (, id \}$       | $\{ ), \$ \}$       |
| $E' \rightarrow +TE' \mid \epsilon$ | $\{ +, \epsilon \}$ | $\{ ), \$ \}$       |
| $T \rightarrow FT'$                 | $\{ (, id \}$       | $\{ +, ), \$ \}$    |
| $T' \rightarrow *FT' \mid \epsilon$ | $\{ *, \epsilon \}$ | $\{ +, ), \$ \}$    |
| $F \rightarrow (E) \mid id$         | $\{ (, id \}$       | $\{ *, +, ), \$ \}$ |



# Another Example of Calculating FIRST and FOLLOW

| Production                      | FIRST | FOLLOW |
|---------------------------------|-------|--------|
| $X \rightarrow Ya$              | { }   | { }    |
| $Y \rightarrow ZW$              | { }   | { }    |
| $W \rightarrow c \mid \epsilon$ | { }   | { }    |
| $Z \rightarrow a \mid bZ$       | { }   | { }    |



# Constructing Predictive Parsing Tables

For each  $A \rightarrow \alpha$  do

1. Add  $A \rightarrow \alpha$  to  $M[A, a]$  for each  $a$  in  $\text{FIRST}(\alpha)$
2. If  $\epsilon$  is in  $\text{FIRST}(\alpha)$ 
  - a. Add  $A \rightarrow \alpha$  to  $M[A, b]$  for each  $b$  in  $\text{FOLLOW}(A)$
  - b. If  $\$$  is in  $\text{FOLLOW}(A)$  add  $A \rightarrow \alpha$  to  $M[A, \$]$
3. Make each undefined entry of  $M$  an error.



# LL(1)

- First "L" - scans input from left to right
- Second "L" - produces a leftmost derivation
- 1 - uses one input symbol of lookahead at each step to make a parsing decision

A grammar whose predictive parsing table has no multiply-defined entries is LL(1).

No ambiguous or left-recursive grammar can be LL(1).





# When Is a Grammar LL(1)?

A grammar is LL(1) iff for each set of productions where  $A \rightarrow \alpha_1 \mid \alpha_2 \mid \dots \mid \alpha_n$ , the following conditions hold.

1.  $\text{FIRST}(\alpha_i)$  intersect  $\text{FIRST}(\alpha_j) = \emptyset$   
where  $1 \leq i \leq n$  and  $1 \leq j \leq n$   
and  $i \neq j$

2. If  $\alpha_i \Rightarrow^* \epsilon$  then

- a.  $\alpha_1, \dots, \alpha_{i-1}, \alpha_{i+1}, \dots, \alpha_n$  does not  $\Rightarrow^* \epsilon$
- b.  $\text{FIRST}(\alpha_j)$  intersect  $\text{FOLLOW}(A) = \emptyset$   
where  $j \neq i$  and  $1 \leq j \leq n$



# Checking If a Grammar is LL(1)

| Production                        | FIRST               | FOLLOW        |
|-----------------------------------|---------------------|---------------|
| $S \rightarrow iEtSS' \mid a$     | $\{ i, a \}$        | $\{ e, \$ \}$ |
| $S' \rightarrow eS \mid \epsilon$ | $\{ e, \epsilon \}$ | $\{ e, \$ \}$ |
| $E \rightarrow b$                 | $\{ b \}$           | $\{ t \}$     |

| Nonterminal | a                 | b                 | e  | i                      | t | \$                        |
|-------------|-------------------|-------------------|--|------------------------|---|---------------------------|
| S           | $S \rightarrow a$ |                   |  | $S \rightarrow iEtSS'$ |   |                           |
| S'          |                   |                   | $S' \rightarrow eS$<br>$S' \rightarrow \epsilon$ |                        |   | $S' \rightarrow \epsilon$ |
| E           |                   | $E \rightarrow b$ |  |                        |   |                           |

So this grammar is not LL(1).



# Bottom-Up Parsing

- Bottom-up parsing
  - attempts to construct a parse tree for an input string beginning at the leaves and working up towards the root
  - is the process of *reducing* the string  $w$  to the start symbol of the grammar
  - at each step, we need to decide
    - when to reduce
    - what production to apply
  - actually, constructs a right-most derivation in reverse

*followed by Fig. 4.25*



# Shift-Reduce Parsing

- Shift-reduce parsing is bottom-up.
- A *handle* is a substring that matches the rhs of a production.
- A *shift* moves the next input symbol on a stack.
- A *reduce* replaces the rhs of a production that is found on the stack with the nonterminal on the left of that production.
- A *viable prefix* is the set of prefixes of right sentential forms that can appear on the stack of a shift-reduce parser

*followed by Fig. 4.35*



# Model of an LR Parser

- Each  $S_i$  is a state.
- Each  $X_i$  is a grammar symbol (when implemented these items do not appear in the stack).
- Each  $a_i$  is an input symbol.
- All LR parsers can use the same algorithm (code).
- The action and goto tables are different for each LR parser.



# LR(k) Parsing

- "L" - scans input from left to right
- "R" - constructs a rightmost derivation in reverse
- "k" - uses k symbols of lookahead at each step to make a parsing decision

Uses a stack of alternating states and grammar symbols. The grammar symbols are optional. Uses a string of input symbols (\$ on end). Parsing table has an action part and a goto part.



# LR (k) Parsing (cont.)

If config ==  $(s_0 X_1 s_1 X_2 s_2 \dots X_m s_m, a_i a_{i+1} \dots a_n \$)$

1. if action  $[s_m, a_i] == \text{shift } s$  then

new config is  $(s_0 X_1 s_1 X_2 s_2 \dots X_m s_m a_i s, a_{i+1} \dots a_n \$)$

2. if action  $[s_m, a_i] == \text{reduce } A \rightarrow \beta$  and

goto  $[s_{m-r}, A] == s$  ( where  $r$  is the length of  $\beta$ ) then

new config is  $(s_0 X_1 s_1 X_2 s_2 \dots X_{m-r} s_{m-r} As, a_i a_{i+1} \dots a_n \$)$

3. if action  $[s_m, a_i] == \text{ACCEPT}$  then stop

4. if action  $[s_m, a_i] == \text{ERROR}$  then attempt recovery

Can resolve some shift-reduce conflicts with lookahead.

ex: LR(1)

Can resolve others in favor of a shift.

ex:  $S \rightarrow iCtS \mid iCtSeS$



# Advantages of LR Parsing

- LR parsers can recognize almost all programming language constructs expressed in context-free grammars.
- Efficient and requires no backtracking.
- Is a superset of the grammars that can be handled with predictive parsers.
- Can detect a syntactic error as soon as possible on a left-to-right scan of the input.





# LR Parsing Example

1.  $E \rightarrow E + T$
2.  $E \rightarrow T$
3.  $T \rightarrow T * F$
4.  $T \rightarrow F$
5.  $F \rightarrow ( E )$
6.  $F \rightarrow \text{id}$

*followed by Fig. 4.37*



# LR Parsing Example

- It produces rightmost derivation in reverse:

$$E \rightarrow E + T \rightarrow E + F \rightarrow E + id$$
$$\rightarrow T + id \rightarrow T * F + id$$
$$\rightarrow T * id + id \rightarrow F * id + id$$
$$\rightarrow id * id + id$$

*followed by Fig. 4.38*



# Calculating the Sets of LR(0) Items

LR(0) item - production with a dot at some position in the right side

Example:

$A \rightarrow BC$  has 3 possible LR(0) items

$A \rightarrow \cdot BC$

$A \rightarrow B \cdot C$

$A \rightarrow BC \cdot$

$A \rightarrow \epsilon$  has 1 possible item

$A \rightarrow \cdot$

3 operations required to construct the sets of LR(0) items:  
(1) closure, (2) goto, and (3) augment

*followed by Fig. 4.32*



# Example of Computing the Closure of a Set of LR(0) Items

## Grammar

$E' \rightarrow E$

$E \rightarrow E + T \mid T$

$T \rightarrow T * F \mid F$

$F \rightarrow ( E ) \mid \text{id}$

## Closure ( $I_0$ ) for $I_0 = \{E' \rightarrow \cdot E\}$

$E' \rightarrow \cdot E$

$E \rightarrow \cdot E + T$

$E \rightarrow \cdot T$

$T \rightarrow \cdot T * F$

$T \rightarrow \cdot F$

$F \rightarrow \cdot ( E )$

$F \rightarrow \cdot \text{id}$



# Calculating Goto of a Set of LR(0) Items

Calculate goto (I,X) where I is a set of items and X is a grammar symbol.

Take the closure (the set of items of the form  $A \rightarrow \alpha X \cdot \beta$ )

where  $A \rightarrow \alpha \cdot X \beta$  is in I.

## Grammar

$E' \rightarrow E$   
 $E \rightarrow E + T \mid T$   
 $T \rightarrow T * F \mid F$   
 $F \rightarrow ( E ) \mid \text{id}$

## Goto ( $I_1, +$ ) for $I_1 = \{E' \rightarrow E \cdot, E \rightarrow E \cdot + T\}$

$E \rightarrow E + \cdot T$   
 $T \rightarrow \cdot T * F$   
 $T \rightarrow \cdot F$   
 $F \rightarrow \cdot ( E )$   
 $F \rightarrow \cdot \text{id}$

## Goto ( $I_2, *$ ) for $I_2 = \{E \rightarrow T \cdot, T \rightarrow T \cdot * F\}$

$T \rightarrow T * \cdot F$   
 $F \rightarrow \cdot ( E )$   
 $F \rightarrow \cdot \text{id}$



# Augmenting the Grammar

- Given grammar  $G$  with start symbol  $S$ , then an augmented grammar  $G'$  is  $G$  with a new start symbol  $S'$  and new production  $S' \rightarrow S$ .

*followed by Fig. 4.33, 4.31*



# Analogy of Calculating the Set of LR(0) Items with Converting an NFA to a DFA

- Constructing the set of items is similar to converting an NFA to a DFA
  - each state in the NFA is an individual item
  - the closure (I) for a set of items is the same as the  $\epsilon$ -closure of a set of NFA states
  - each set of items is now a DFA state and goto (I,X) gives the transition from I on symbol X

*followed by Fig. 4.31, A*



# Sets of LR(0) Items Example

$$S \rightarrow L = R \mid R$$
$$L \rightarrow *R \mid \text{id}$$
$$R \rightarrow L$$

*followed by Fig. 4.39*





# Constructing SLR Parsing Tables

Let  $C = \{I_0, I_1, \dots, I_n\}$  be the parser states.

1. If  $[A \rightarrow \alpha \cdot a \beta]$  is in  $I_i$  and  $\text{goto}(I_i, a) = I_j$  then set action  $[i, a]$  to 'shift  $j$ '.
2. If  $[A \rightarrow \alpha \cdot]$  is in  $I_i$ , then set action  $[i, a]$  to 'reduce  $A \rightarrow \alpha$ ' for all  $a$  in the  $\text{FOLLOW}(A)$ .  $A$  may not be  $S'$ .
3. If  $[S' \rightarrow S \cdot]$  is in  $I_i$ , then set action  $[i, \$]$  to 'accept'.
4. If  $\text{goto}(I_i, A) = I_j$ , then set  $\text{goto}[i, A]$  to  $j$ .
5. Set all other table entries to 'error'.
6. The initial state is the one holding  $[S' \rightarrow \cdot S]$ .

*followed by Fig. 4.37*



# Using Ambiguous Grammars

|                              |            |                                      |
|------------------------------|------------|--------------------------------------|
| 1. $E \rightarrow E + E$     |            | $E \rightarrow E + T \mid T$         |
| 2. $E \rightarrow E * E$     | instead of | $T \rightarrow T * F \mid F$         |
| 3. $E \rightarrow ( E )$     |            | $F \rightarrow ( E ) \mid \text{id}$ |
| 4. $E \rightarrow \text{id}$ |            |                                      |

See Figure 4.48.

Advantages:

Grammar is easier to read.

Parser is more efficient.

*followed by Fig. 4.48*



# Using Ambiguous Grammars (cont.)

Can use precedence and associativity to solve the problem.

See Fig 4.49.

shift / reduce conflict in state  $\text{action}[7,+]=(s4,r1)$

$s4 = \text{shift } 4 \quad \text{or} \quad E \rightarrow E \cdot + E$

$r1 = \text{reduce } 1 \quad \text{or} \quad E \rightarrow E + E \cdot$

$\text{id} + \text{id} + \text{id}$

↑ cursor here

$\text{action}[7,*]=(s5,r1)$

$\text{action}[8,+]=(s4,r2)$

$\text{action}[8,*]=(s5,r2)$

*followed by Fig. 4.49*



# Another Ambiguous Grammar

0.  $S' \rightarrow S$

1.  $S \rightarrow iSeS$

2.  $S \rightarrow iS$

3.  $S \rightarrow a$

See Figure 4.50.

$\text{action}[4,e]=(s5,r2)$

*followed by Fig. 4.50, 4.51*



# Ambiguities from Special-Case Productions

$E \rightarrow E \text{ sub } E \text{ sup } E$

$E \rightarrow E \text{ sub } E$

$E \rightarrow E \text{ sup } E$

$E \rightarrow \{ E \}$

$E \rightarrow c$



# Ambiguities from Special-Case Productions (cont)

1.  $E \rightarrow E \text{ sub } E \text{ sup } E$

2.  $E \rightarrow E \text{ sub } E$

3.  $E \rightarrow E \text{ sup } E$

4.  $E \rightarrow \{ E \}$

5.  $E \rightarrow c$

$\text{FIRST}(E) = \{ \{', c \}$

$\text{FOLLOW}(E) = \{ \text{sub}, \text{sup}, \}', \$ \}$

sub, sup have equal precedence  
and are right associative

*followed by Fig. B*



# Ambiguities from Special-Case Productions (cont)

1.  $E \rightarrow E \text{ sub } E \text{ sup } E$

2.  $E \rightarrow E \text{ sub } E$

3.  $E \rightarrow E \text{ sup } E$

4.  $E \rightarrow \{ E \}$

5.  $E \rightarrow c$

$\text{FIRST}(E) = \{ \{'\}, c \}$

$\text{FOLLOW}(E) = \{ \text{sub}, \text{sup}, \}'\}, \$ \}$

sub, sup have equal precedence  
and are right associative

$\text{action}[7, \text{sub}] = (\text{s4}, \text{r2})$

$\text{action}[8, \text{sub}] = (\text{s4}, \text{r3})$

$\text{action}[11, \text{sub}] = (\text{s5}, \text{r1}, \text{r3})$

$\text{action}[11, \}] = (\text{r1}, \text{r3})$

$\text{action}[7, \text{sup}] = (\text{s10}, \text{r2})$

$\text{action}[8, \text{sup}] = (\text{s5}, \text{r3})$

$\text{action}[11, \text{sup}] = (\text{s5}, \text{r1}, \text{r3})$

$\text{action}[11, \$] = (\text{r1}, \text{r3})$

*followed by Fig. C*



# YACC

Yacc source program

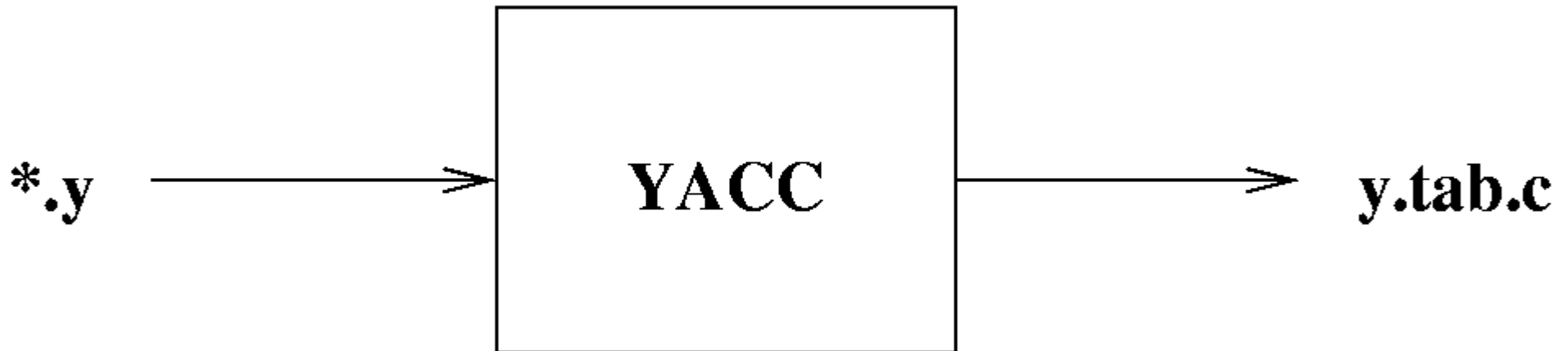
declaration

% %

translation rules

% %

supporting C-routines



*followed by Fig. 4.57*





# YACC Declarations

- In declarations:

- Can put ordinary C declarations in

% {

...

% }

- Can declare tokens using

- %token
    - %left
    - %right

- Precedence is established by the order the operators are listed (low to high).



# YACC Translation Rules

- Form

$A : \text{Body} ;$

where  $A$  is a nonterminal and  $\text{Body}$  is a list of nonterminals and terminals.

- Semantic actions can be enclosed before or after each grammar symbol in the body.
- Yacc chooses to shift in a shift/reduce conflict.
- Yacc chooses the first production in a reduce/reduce conflict.



# Yacc Translation Rules (cont.)

- When there is more than one rule with the same left hand side, a '|' can be used.

A : B C D ;

A : E F ;

A : G ;

=>

A : B C D

| E F

| G

;



# Example of a Yacc Specification

```
%token IF ELSE NAME          /* defines multicharacter tokens */
%right '='                   /* low precedence, a=b=c shifts */
%left '+' '-'                /* mid precedence, a-b-c reduces */
%left '*' '/'                /* high precedence, a/b/c reduces */
%%
stmt  : expr ';'
      | IF '(' expr ')' stmt
      | IF '(' expr ')' stmt ELSE stmt
      ;      /* prefers shift to reduce in shift/reduce conflict */
expr  : NAME '=' expr        /* assignment */
      | expr '+' expr
      | expr '-' expr
      | expr '*' expr
      | expr '/' expr
      | '-' expr %prec '*' /* can override precedence */
      | NAME
      ;
%% /* definitions of yylex, etc. can follow */
```



# Yacc Actions

- Actions are C code segments enclosed in { } and may be placed before or after any grammar symbol in the right hand side of a rule.
- To return a value associated with a rule, the action can set \$\$.
- To access a value associated with a grammar symbol on the right hand side, use \$i, where i is the position of that grammar symbol.
- The default action for a rule is  

```
{ $$ = $1; }
```

*followed by Fig. 4.58, 4.59*



# Syntax Error Handling

- Errors can occur at many levels
  - lexical - unknown operator
  - syntactic - unbalanced parentheses
  - semantic - variable never declared
  - logical - dereference a null pointer
- Goals of error handling in a parser
  - detect and report the presence of errors
  - recover from each error to be able to detect subsequent errors
  - should not slow down the processing of correct programs



# Syntax Error Handling (cont.)

- Viable-prefix property - detect an error as soon as see a prefix of the input that is not a prefix of any string in the language.



# Error-Recovery Strategies

- Panic- mode
  - skip until one of a synchronizing set of tokens is found (e.g. ';', "end"). Is very simple to implement but may miss detection of some error (when more than one error in a single statement)
- Phase- level
  - replace prefix of remaining input by a string that allows the parser to continue. Hard for the compiler writer to anticipate all error situations





# Error-Recovery Strategies (cont...)

- Error productions
  - augment the grammar of the source language to include productions for common errors. When production is used, an appropriate error diagnostic would be issued. Feasible to only handle a limited number of errors.
- Global correction
  - choose minimal sequence of changes to allow a least-cost correction. Too costly to actually be implemented in a parser. Also the closest correct program may not be what the programmer intended.