

Homework 4

Chapter 5

26.

28. a, b

35.

Class 1. a) Convolve $x(t) = \left(\frac{1}{T_0}\right) \text{rect}\left(\frac{t}{T_0}\right)$ with $h(t) = u(t) \frac{1}{RC} e^{-\frac{t}{RC}}$ to find the output $y(t)$, for

a) $T_0 = 0.1$ and $RC = 0.5$ Plot the result.

b) $T_0 = 1$ and $RC = 0.5$. Plot the result.

Confirm your answer with Approximate Impulse Response @

http://www.ittc.ku.edu/~frost/EECS_360/Mathematica-360/Impulse_Examples.cdf

Also look at Convolution with a Rectangular Pulse @

<http://demonstrations.wolfram.com/ConvolutionWithARectangularPulse/>

c) Is the result from part a) close to $h(t)$, why?

d) Convolve $x(t) = \left(\frac{1}{T_0}\right) \text{rect}\left(\frac{t}{T_0}\right)$ with $h(t) = u(t-1) \frac{1}{RC} e^{-\frac{(t-1)}{RC}}$ for $T_0 = 1$ and $RC = 0.5$. Plot the result.

c) What is the relationship between the results in parts b) and d) above?

Hint: $\text{rect}(t) = u(t+0.5) - u(t-0.5)$. The step response of a system is $h_{-1}(t) = h(t) * u(t)$, the step response is discussed on pp 176. Convolution is used to represent linear time invariant systems.

Class 2. Convolve $h(n) = .1(u(n) - u(n-10))$ with $x(n) = u(n) - u(n-10)$ Plot the result.

Confirm your answers with [Discrete-Time Convolution.](#) @

<http://demonstrations.wolfram.com/DiscreteTimeConvolution/>

Class 3. Let $x(n) = 0, 1, 2$ for $n = 0, 1, 2$ and $h(n) = 3, 2, 1$ for $n = 0, 1, 2$. Convolve $x(n)$ with $h(n)$ and plot the result. Confirm your answer with [Convolution Sum.](#) @

<http://demonstrations.wolfram.com/ConvolutionSum/>

Class 4. Convolve $\text{Rect}\left[\frac{t+15}{2}\right] + \text{Rect}\left[\frac{t-15}{2}\right]$ with $\text{Rect}\left[\frac{t+10}{2}\right] + \text{Rect}\left[\frac{t-10}{2}\right]$. Plot the result. (Hint: see problem Chapter 5-5c)

Class 5. Convolve $x(t) = t^2 \text{rect}(t - .5)$ and $h(t) = u(t) e^{-t}$.

Class 6. The system input, $x(t) = \frac{u(t-1)\exp(-(t-.5))}{\exp(-.5)} + \text{rect}(t - .5)$ and impulse response, $h(t) = \text{rect}(t-.5)$, are given below. Find the system output.

