

EECS 361
Homework #2

1. Section 2.5 Participation activities

- 2.5.2: Unit step function.
- 2.5.4: Ramp function.
- 2.5.5: Triangle waveform synthesized from ramps.
- 2.5.6: Rectangular (rect) function.
- 2.5.8: Impulse function.
- 2.5.9: Sampling property of the impulse function.
- 2.5.10: Time-scaling of impulse function sampling integrals.
- 2.5.11: Exponential function.
- 2.5.12: Exponential functions.

2. Challenge activity

- 2.5.1: Nonperiodic waveforms 3.

3. Given $x(t) = 100u(t)e^{-\frac{t}{50}}$ find how long it takes $x(t)$ to be reduced to 50% of its peak value, that it find it half-life value.

4. Plot the following functions over a range of t from -10 to 10.

a. $x_1(t) = -4u(t+4)$

b. $x_2(t) = -4u(t-4)$

c. $x_1(t) - x_2(t)$

5. Solve the following.

a. $\int_{-\infty}^{\infty} \delta(\tau) e^{-2\tau} d\tau$

b. $\int_{-\infty}^{\infty} \delta(\tau - 0.2) u(\tau) e^{-2\tau} d\tau$

c. $\int_{-\infty}^{\infty} \delta(\tau - .8) u(\tau) e^{-2\tau} d\tau$

d. $\int_{-\infty}^{\infty} \delta(\tau - t) u(\tau) e^{-2\tau} d\tau$

6. Plot and compare these three signals. Explain their similarities and differences.

$$x_1(t) = 2\cos(2\pi 1000t), x_2(t) = 2\cos\left(2\pi 1000\left(t - \frac{1}{8000}\right)\right), x_3(t) = 2\cos\left(2\pi 50t - \frac{\pi}{4}\right)$$

7. Let

$$x(t) = \sum_{k=-n}^n 6 \operatorname{rect}\left(\frac{t - 4k}{2}\right) - 3$$

a. For $n=2$ plot $x(t)$

b. Sketch $x(t)$ as $n \rightarrow \infty$, in this case is $x(t)$ periodic, if so what is the period.

8. Plot

$$x(t) = \sum_{n=1}^5 \frac{1}{n\pi} \sin(2\pi nt) \text{ for } -3 < t < 3$$

9.

a. Given a sequence of 4 bits are represented by voltage levels $a_i = \{1, -1, 1, -1\}$; plot a binary signal $x(t)$,

$$x(t) = \sum_{n=1}^4 a_n \operatorname{rect}(t - n + 0.5)$$

b. Binary Phase Keyed (BPSK) modulation is used to modulate binary information onto a radio frequency carrier. A BPSK signal is given as $x(t) \cos(2\pi f_c t)$. Plot (RF)

$$x_{\text{RF-BPSK}}(t) = \sum_{n=1}^4 a_n \text{rect}(t - n + 0.5) \cos(2\pi 3t)$$

c. A modulation using amplitude shift keying (ASK) signal is generated by changing a_i to $b_i = \{1, 0, 1, 0\}$. Plot

$$x_{\text{RF-ASK}}(t) = \sum_{n=1}^4 b_n \text{rect}(t - n + 0.5) \cos(2\pi 3t)$$

10. Plot for $-4 < t < 4$

a. $\frac{\sin(\pi t)}{\pi t}$ (L'Hôpital's rule can be used to show that $\frac{\sin(\pi t)}{\pi t} \Big|_{t=0} = 1$)

b. $\frac{\sin(2\pi t)}{2\pi t}$