

EECS 361
Homework #5

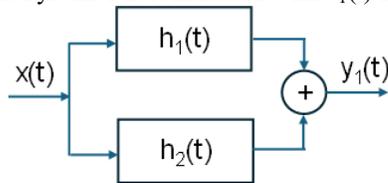
1. Section 3.5 Participation Activities

- 3.5.1: Convolution properties.
- 3.5.2: Convolution of two delayed rectangular pulses, using the properties.
- 3.5.3: Convolution properties.
- 3.5.4: Common convolutions.
- 3.5.5: Using convolution properties.

2. (Concepts: LTI systems in parallel and series)

Two LTI systems have impulse responses of $h_1(t) = \text{rect}\left(\frac{t-10}{5}\right)$ and $h_2(t) = \text{rect}\left(\frac{t+10}{5}\right)$.

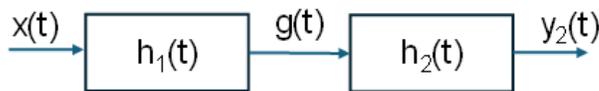
a. System 1 is constructed with $h_1(t)$ and $h_2(t)$ as shown below.



Find the impulse response of System 1.

System 1

b. System 2 is constructed with $h_1(t)$ and $h_2(t)$ as shown below.



Find the impulse response of System 2.

System 2

c. For $x(t) = \text{rect}\left(\frac{t-20}{5}\right) + \text{rect}\left(\frac{t+20}{5}\right)$ find and plot the output, $y_1(t)$ of System 1.

d. For $x(t) = \delta(t+12) + \delta(t) + \delta(t-12)$ find and plot the system output $y_2(t)$ in System 2.

3. (Concept: Convolution with a step function)

For $x(t) = 4\sin(\pi t)\text{rect}(t-.5)$ and $h(t) = u(t)$ find $h(t)*x(t)$ and plot.

4. Section 3.6 Participation Activities

- 3.6.1: BIBO stability and causality.
- 3.6.2: BIBO stability.
- 3.6.3: BIBO stability for complex exponential (sinusoidal) signals.

5. (Concept: convolution of exponential signals)

Find and plot the convolution of the following function $x(t) = 2u(t)e^{-t/2}$ and $h(t) = 4u(t)e^{-t/4}$.

6. (Concept: Determining causality and stability from the impulse response)

- a. $h(t) = 100 \text{rect}(t + 5)$ is a stable system, TRUE or FALSE
- b. $h(t) = 100 \text{rect}(t + 5)$ is a causal system, TRUE or FALSE
- c. $h(t) = 100 \text{rect}(t + 2)e^{t/3}$ is a stable system, TRUE or FALSE
- d. $h(t) = 100 \text{rect}(t + 2)e^{t/3}$ is a causal system, TRUE or FALSE
- e. $h(t) = 100 \text{rect}(t - 2)e^{t/3}$ is a stable system, TRUE or FALSE
- f. $h(t) = 100 \text{rect}(t - 2)e^{t/3}$ is a causal system, TRUE or FALSE
- g. $h(t) = 100 u(t)e^{t/3}$ is a stable system, TRUE or FALSE
- h. $h(t) = 100 u(t)e^{t/3}$ is a causal system, TRUE or FALSE

7. (Concept: Using a comb function and convolving a comb function with a prototype pulse)

A comb function or infinite impulse train is defined as $\delta_T(t) = \sum_{k=-\infty}^{\infty} \delta(t-kT)$.

Let $\delta_3(t) = \sum_{k=-\infty}^{\infty} \delta(t-3k)$ and $g(t) = \text{tri}(t)$,

- a. Find $y(t) = g(t)*\delta_3(t)$ and plot $y(t)$.
- b. Is $y(t)$ periodic, if so what is the period?

Hint: Sketch a plot of $\delta_4(t)$.